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A REDESIGNED INSTRUMENT AND NEW DATA ANALYSIS METHOD USED
TO MEASURE THE SIZE AND VELOCITY OF HYDROMETEORS

by
Bryson Evan Winsky

A thesis submitted in partial fulfillment
of the requirements for the Master of
Science degree in Civil and Environmental Engineering
in the Graduate College of
The University of Iowa

July 2012

Thesis Supervisor: Professor William E. Eichinger

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Graduate College
The University of Iowa
Iowa City, Iowa

CERTIFICATE OF APPROVAL

MASTER'S THESIS

This is to certify that the Master's thesis of

Bryson Evan Winsky

has been approved by the Examining Committee
for the thesis requirement for the Master of Science
degree in Civil and Environmental Engineering at the July 2012 graduation.

Thesis Committee: _____
William E. Eichinger, Thesis Supervisor

Allen Bradley

Anton Kruger

To My Family and Friends

Strive for perfection in everything you do. Take the best that exists and make it better.
When it does not exist, design it.

Sir Henry Royce
British Engineer (1863-1933)

ACKNOWLEDGMENTS

First, I would like to thank my family and friends for their support and patience during this project. Also, I would like to thank Bill for his support during the duration of this project. He offered many ideas and solutions to problems that made this project possible.

TABLE OF CONTENTS

| | |
|----------------------------------------------------|----|
| LIST OF TABLES | iv |
| LIST OF FIGURES | v |
| CHAPTER 1 INTRODUCTION | 1 |
| CHAPTER 2 AVAILABLE TECHNOLOGY | 3 |
| Impact Disdrometer | 3 |
| Issues | 4 |
| Two-Dimensional Video Disdrometer | 4 |
| Issues | 6 |
| Light Sheet Disdrometer | 6 |
| Issues | 7 |
| CHAPTER 3 INSTRUMENT DESIGN | 9 |
| Introduction..... | 9 |
| Instrument Housing | 10 |
| Internal Components..... | 11 |
| Cost of Instrument | 12 |
| CHAPTER 4 DATA ANALYSIS | 14 |
| Introduction..... | 14 |
| Raw Data Acquisition..... | 14 |
| Data Analysis..... | 18 |
| Velocity Calculation..... | 19 |
| Theoretical Diameter Calculation..... | 19 |
| Half-Max Diameter Calculation | 21 |
| Limitation of Half-Max Diameter Calculations | 24 |
| CHAPTER 5 INSTRUMENT VALIDATION..... | 28 |
| Introduction..... | 28 |
| Steel Sphere Experiment..... | 28 |
| Steel Sphere Experiment Results..... | 29 |
| Steel Sphere Experiment Discussion..... | 31 |
| Drip Experiment | 33 |
| Drip Experiment Results | 33 |
| Drip Experiment Discussion..... | 35 |
| Conclusions of Lab Experiments..... | 36 |
| CHAPTER 6 OUTDOOR TESTING | 38 |
| Instrument Location..... | 38 |
| Data Sets | 39 |
| Instrument Comparison | 41 |
| Velocity..... | 43 |
| Discussion..... | 45 |

| | |
|-----------------------------------|----|
| Outdoor Testing Conclusions | 48 |
| CHAPTER 7 CONCLUSION..... | 50 |
| Issues to Be Addressed | 52 |
| BIBLIOGRAPHY..... | 54 |

LIST OF TABLES

| | |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| Table 1 - The itemized prices of the materials and components used to construct the instrument. | 13 |
| Table 2 -The resulting velocities for each diameter tested. | 29 |
| Table 3 - The resulting diameters for each diameter tested. | 30 |
| Table 4 - Average results from Drip Experiment. | 35 |
| Table 5 - The number of triggers and errors associated with each rain event. | 46 |
| Table 6 - A table breaking down the number of simultaneous drops in the sample area and the number of drops smaller than 0.90 mm not included in the DSD. | 47 |

LIST OF FIGURES

| | |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| Figure 1 - Joss - Waldvogel Impact Disdrometer RD 80..... | 3 |
| Figure 2 - The three main components of the Two Dimensional Video Disdrometer | 5 |
| Figure 3 - Conceptual Drawing of 2DVD..... | 5 |
| Figure 4 - A Thies Disdrometer | 7 |
| Figure 5 - A typical pulsed signals as raindrops pass through the light sheet of an optical disdrometer..... | 8 |
| Figure 6 - The improved prototype..... | 9 |
| Figure 7 - The design of the housing constructed from copper. The laser head and detector head are made out of 2 ½ inch copper tubing. The frame is constructed from ½ inch copper tubing. The base is constructed from solid stock of 1 inch thick copper..... | 10 |
| Figure 8 - The layout of the electrical and optical components located inside the laser head and detector head..... | 11 |
| Figure 9 - A sample of raw data as a steel sphere passes through the sample area. The two pulsed signals correspond to the raindrop passing through and blocking the first laser sheet and second laser sheet, respectively..... | 14 |
| Figure 10 - Cosine functions fitted to the pulsed signals generated by a steel sphere. If the sheet lasers were infinitely thin the pulsed signals would fit the cosine curves. | 15 |
| Figure 11 - An example of a pulsed signal produced by a sphere with a diameter smaller than the thickness of a laser sheet..... | 16 |
| Figure 12 - An example of a pulsed signal produced by a spherical hydrometeor larger than the thickness of the laser sheet. | 17 |
| Figure 13 - An example of the tails produced by a spherical hydrometeor passing through a laser sheet that has a thickness. The red portions of the signals are the tails..... | 17 |
| Figure 14 - An inverted and normalized data sample showing the parameters obtained from the raw data. The lag time (t_{lag}) is the time it takes the hydrometeor to travel from the center of one laser sheet to the center of the other. The time of attenuation (t_{att}) is the cumulative time it takes a hydrometeor to pass through one laser sheet. The time of attenuation can be measured twice from the two pulsed signals. t_{att1} corresponds to the first pulsed signal, and t_{att2} corresponds to the second pulsed signal. | 18 |

| | |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| Figure 15 - An inverted and normalized data sample showing the parameters obtained from the raw data. The lag time (t_{lag}) is the time it takes the hydrometeor to travel past the two sheet lasers. The half max time of attenuation ($t_{1/2att}$) is the time between the half maximum of the signal. The half max time of attenuation can be measured two times from each pulsed signal. $t_{1/2att1}$ corresponds to the first pulsed signal, and $t_{1/2att2}$ corresponds to the second pulsed signal..... | 21 |
| Figure 16 - 1st pulsed signal data reduction curve. The drop diameter is obtained by calculating the half-max diameter using the hydrometeors velocity and the half-max time of attenuation from the first pulsed signal $t_{1/2att1}$ | 22 |
| Figure 17 - 2nd pulsed signal data reduction curve. The drop diameter is obtained by calculating the half- max diameter using the hydrometeors velocity and the half-max time of attenuation from the second pulsed signal $t_{1/2att2}$ | 23 |
| Figure 18 - Schematic of a drop with a radius smaller than or equal to the laser sheet thickness exiting the laser sheet. The amount of light being attenuated corresponds to the projected area remaining in the laser sheet..... | 24 |
| Figure 19 - A model fitted to the two pulsed signals used to estimate the radius produced by a hydrometeor with a radius equal to or smaller than the laser sheet thicknesses. | 26 |
| Figure 20 - An example of a stair step signal produced by a small hydrometeor..... | 27 |
| Figure 21 - Steel Sphere Experimental Setup. The steel spheres were dropped from a height of 0.396 meters. | 29 |
| Figure 22 - The average fractional errors associated with each diameter tested. The average fractional error decreases with increasing diameters. | 30 |
| Figure 23 - Drip Experiment Setup..... | 34 |
| Figure 24 - Results of the 22 trials recorded during the drip experiment. | 35 |
| Figure 25 - A map showing the location where the new prototype was placed outside to record precipitation events..... | 38 |
| Figure 26 - The drop size distribution recorded during a thunderstorm on February 29th..... | 39 |
| Figure 27 - A snow event captured on February 29th (14:00 - 17:00hrs). The size of the snowflakes has not been studied and therefore should not be valued with any confidence..... | 40 |
| Figure 28 - The DSD from a light rain on March 12th..... | 40 |
| Figure 29 - A comparison of Precipitation Rates between a tipping bucket and the new prototype. It thunder stormed between 0:00 and 2:00 hours and it snowed between 14:00 and 17:00 hours..... | 41 |
| Figure 30 - The rain rates measured by the new prototype and tipping bucket on March 12 th , 2012. The rain event was categorized as light rain. | 42 |

| | |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| Figure 31 - A comparison of the measured rain rates captured by the prototype and tipping bucket during the rain event on February 29 th , 2012. The instruments are in better agreement at lower rain rates..... | 42 |
| Figure 32 - A comparison of the measured velocities during a thunderstorm captured on February 29th, 2012 against the theoretical Gunn and Kinzer Relationship. The scatter of the measured data is mostly likely due to the dynamic environment in which the measurements were taken..... | 43 |
| Figure 33 - The velocities of snowflakes compared against the Gunn & Kinzer Relationship..... | 44 |
| Figure 34 - The velocities measured during the March 12th rain event compared against the Gunn & Kinzer Relationship..... | 44 |
| Figure 35 - An example of another drop entering the sample area during the same window of time a measurement takes place..... | 46 |

CHAPTER 1

INTRODUCTION

Precipitation measurements have a broad range of applications in meteorology, hydrology, agriculture, and other sciences. More specifically, accurate precipitation measurements lead to better predictions of floods, droughts, erosion, and crop yields. Precipitation measurements are made at a wide range of temporal and spatial scales. The spatial scale ranges from hundreds of kilometers to single hydrometeors, and the temporal scales range from minutes to years. Therefore, it is not surprising that much time, money, and effort has been put forth to increase our ability to measure precipitation.

Precipitation is measured with several different instruments. The simplest of the instruments is the typical house-hold rain gauge. These gauges are usually constructed from a cylindrical tube that has a length scale on it. The instrument gives a point measurement of the total accumulation of a storm event. On the other end of the spectrum, the rainfall radar is a technological advanced method that measures areal precipitation with temporal resolutions on the order of minutes. Conceptually, radars transmit pulses of microwave energy that scatter from targets, which in this case are rain drops. Some of the energy that is scattered from the raindrops is scattered back to the receiver. The receiver measures the power of the return signal also known as the reflectivity (Z). The reflectivity can be used to estimate the amount of rainfall (R). The relationship between the reflectivity and estimated rainfall is known as the Z-R relationship. The reflectivity depends strongly on the drop size distributions (DSD) of the rainfall events, a parameter that can have significant variability. In order to obtain better estimates from radar measurements, the DSD during precipitation events needs to be accurately measured. In particular, multiple reliable measurements are needed to study the spatial and temporal variations of the DSD.

Additionally, accurate measurements of the DSD and drop velocities would potentially benefit erosion research. The momentum of individual raindrops is the product of the

mass(volume) and velocity of the raindrops and is responsible for dislodging soil particles.

Dislodgement of soil particles from a compacted surface is the beginning of the erosion process.

Disdrometers are commonly used to measure the DSD during precipitation events. A disdrometer is an instrument that measures the size of individual hydrometeors. Some disdrometers have the capability to measure not only the size of hydrometeors, but also, the velocity and shape of hydrometeors. Joss and Waldvogel invented the first impact disdrometer in 1967 (Tokay et al., 2002). Since the invention of the first impact disdrometer, the 2-Dimensional Video Disdrometers (2DVD) and optical disdrometers have been built. Studies by (Tokay, et al, 2001) and (Frasson et al, 2011) have evaluated the uncertainties of the impact, 2DVD, and optical disdrometers. They have found that there are many uncertainties associated with collecting and analyzing data with each of these instruments. The instruments will be discussed more in the Chapter 2.

The spatial and temporal variations of the DSD during a rainstorm can be measured with a network of disdrometers distributed throughout an area. However, due to the high cost, and lack of consistency of the current disdrometers, DSD measurements suffer. Thus, there is still a need to for an instrument that is durable, reliable in harsh weather environments, calibration free, inexpensive and able to accurately measure drop sizes.

The primary goal of this project is to redesign and build an instrument previously designed by Michael Cloos to fit the criteria described previously. The following chapters will discuss the commercially available disdrometers, the new instrument design, a new data analysis method, and the performance of the new instrument.

CHAPTER 2

AVAILABLE TECHNOLOGY

Impact, video, and light sheet (optical) disdrometers are the three primary types of disdrometers. In this chapter, a brief description of each type will be discussed.

Impact Disdrometer

The Joss-Waldvogel Disdrometer (JWD) RD 80 will be used as an example of an impact disdrometer in this section. The JWD has two main components, the sensor and the processor as shown in Figure 1. The sensor is an electrical mechanical unit that measures the vertical

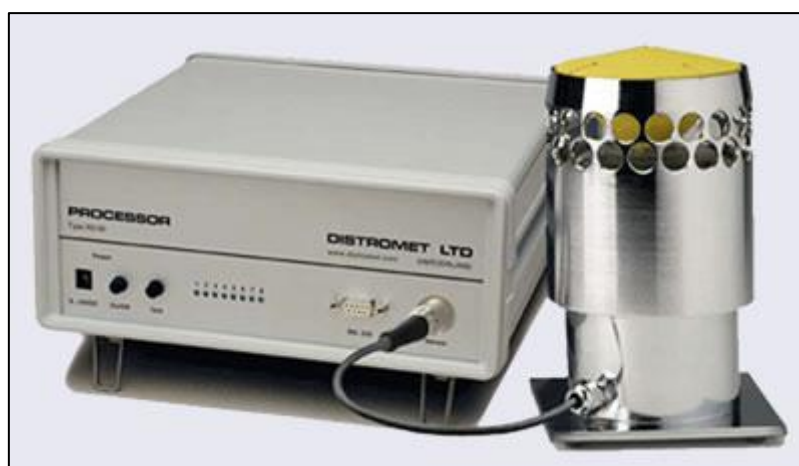


Figure 1 - Joss - Waldvogel Impact Disdrometer RD 80 (www.distromet.com).

momentum of raindrops as they impact the sensor. The sensor transforms the momentum into a pulsed signal that is measured by the processor. At the processor, the amplitude of pulsed signal is measured. The amplitude of the pulsed signal is related to the size of the drop that impacted the sensor. The processor sorts the drop diameters into 127 channels, each representing the number of drops in a size interval, and further compresses the data into 20 classes. The 20

classes are then averaged every minute and stored. The DSDs are output in the form of a table, graph, or plot using DISDRODATA, the JWD software.

According to the Disdrometer RD 80 manufacture specifications the area of the sensor is 50 cm^2 . The specifications also report that the RD 80 is able to measure drop diameters within a range of 0.3 to 5 millimeters within 5 % of the raindrop's true diameter.

Issues

Wind and splatter from other raindrops impacting the instrument produce small disturbances in the JWD sensor which signal false raindrops that are processed and included in the measured DSD. Additionally, if the sensor is continuously vibrating, it increases the smallest diameter at which drop sizes can be detected. Therefore, small raindrops are under sampled, and the DSD is skewed toward larger drop sizes (List, 1988). The continuous vibrations occur during heavy rain from splashing drops and windy conditions. Furthermore, the upper limit, 5 to 5.5 millimeters diameters, was recognized to be another source of error during rain events that have large rain drops (Kruger et al. 2002). Errors are also acquired when processing the data since the measured drop diameters are sorted into 20 classes.

Two-Dimensional Video Disdrometer

The Two-Dimension Video Disdrometer (2DVD) has three main components as shown in Figure 2. The first component is the sensor which houses the cameras, light sources and optics. The second is the outdoor electronics unit which houses the computer that operates the components in the sensor. The third component is the indoor personal computer where the raw data is transferred.

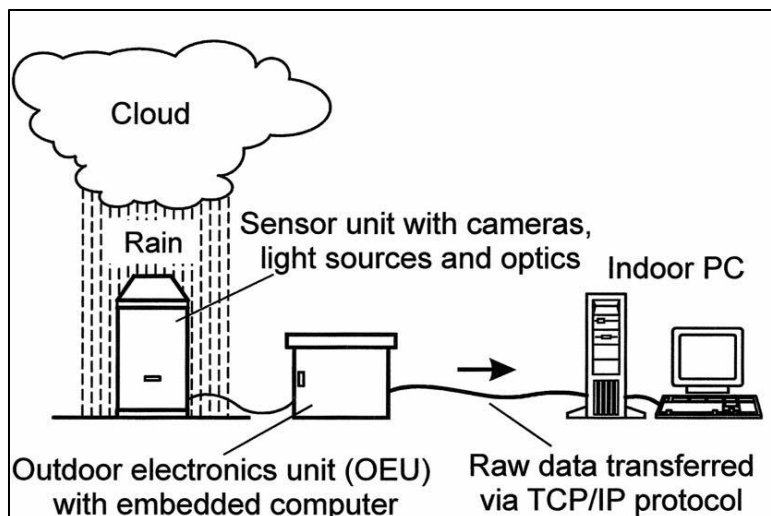


Figure 2 - The three main components of the Two Dimensional Video Disdrometer (Kruger & Krajewski, 2001).

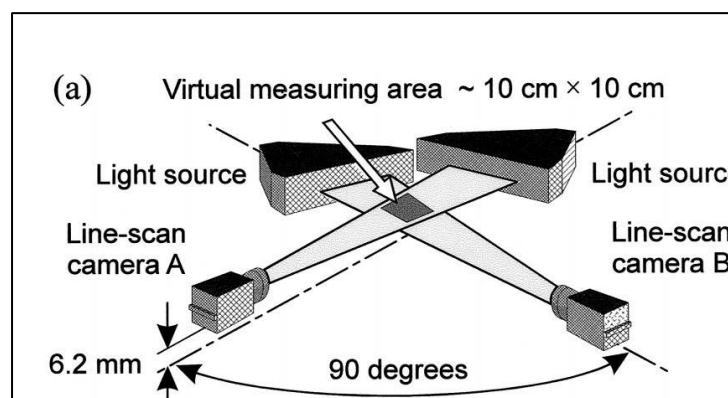


Figure 3 - Conceptual Drawing of 2DVD (Kruger & Krajewski, 2001).

The 2DVD operates by projecting two light sheets onto two line scan cameras. The cameras take images of raindrops at 34.1 kHz as they fall through to two light sheets separated by a vertical distance of 6.2 millimeters as shown in Figure 3 (Kruger and Krajewski, 2001). From the images, the velocity, diameter, and shape of the raindrops can be measured. The

smallest drop the 2DVD can reliably measure is 0.2mm with a measured drop sizes accuracy of $\pm 0.2\text{mm}$ (Tokay et al, 2002).

Issues

The main shortcoming of the 2DVD is the size of the instrument. First, the size of the instrument creates uncertainties during the data collection process. Drops impacting the structure of the sensor break up into small drops and fall through the sample area. Splatter from the broken drops cause the 2DVD to overestimate the number of small to medium size drops being measured during a rain event (Kruger and Krajewski, 2001). Also, since the profile of the instrument is large, the air flow around the instrument is altered. Consequently, the alterations in the air flow change the trajectories of hydrometeors. The trajectories of small drops can be altered to the point that the small drops do not enter the sampling area (Nespor, Krajewski, & Kruger, 2000). Secondly, the large size of the sensor, outdoor electronics unit and computer make it make it difficult to transport.

The cost of the 2DVD is another shortcoming of this instrument. The 2DVD is 3 to 5 times more expensive than other disdrometers. Due to the high cost, multiple instruments are seldom deployed simultaneously, which limits the ability of researchers trying to study the spatial distribution of precipitation events.

Light Sheet Disdrometer

Many new single light sheet disdrometers can be found in the literature. Light sheet disdrometers are the newest technology available. Light sheet disdrometers have two components, a light source and a light detector. A commercially available light sheet disdrometer known as the Thies Disdrometer is shown in Figure 4. The light source is commonly a laser beam that is transformed into a single laser sheet. The laser sheet then travels to the light detector located in the electrical box where voltage measurements are taken. Blockage of laser light as a hydrometeor passes through the sampling area produces a decrease in voltage readings. The decrease in voltage forms a pulsed signal. A sample voltage reading is shown in Figure 5. The



Figure 4 - A Thies Disdrometer (<http://www.thiesclima.com/disdrometer.html>)

velocity of the hydrometeor is calculated by dividing the thickness of the laser sheet by the time interval for one drop. The maximum amplitude of the signal is used to measure the size of hydrometeor. The amplitude of the signal is related to the amount of light blocked by the raindrop.

Issues

The non-uniform energy density of the light sheet is a major source of error. Since the energy density is non-uniform, the amplitude and duration of the signals are different depending on the location the drop passes through the light sheet. (Fransson et al., 2011) found that drops are overestimated when drops fall directly through the center of the sheet laser and underestimated drop diameters at the edge of the sheet lasers. Additionally, if the lenses of the instrument become dirty, or scratched, the sheet laser light will become non-uniform producing more error in the diameter and velocity measurements. As the instrument ages, the intensity of the laser will change, as will the sensitivity of the detector, necessitating frequent recalibration.

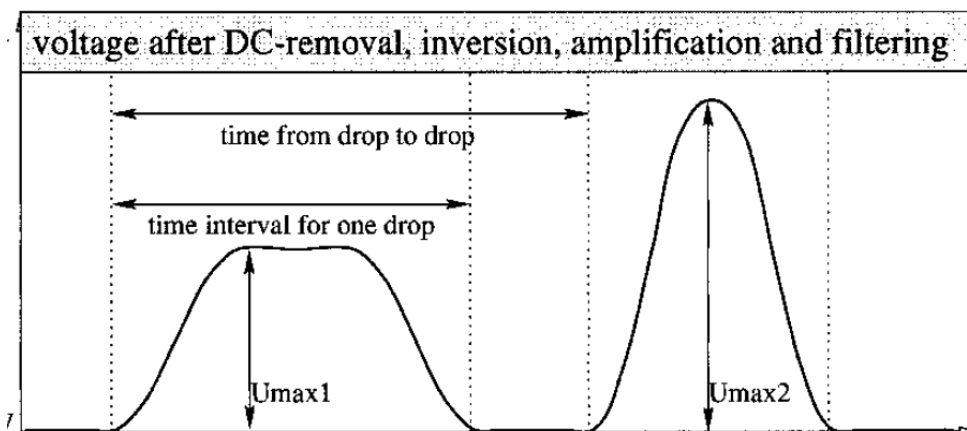


Figure 5 - A typical pulsed signals as raindrops pass through the light sheet of an optical disdrometer (Löffler-Mang, 1998).

Also, for instruments of this type, drops splashing off of the instrument into the sample area and disturbances in the air flow surrounding the instrument produce errors when measuring the drop size distribution.

CHAPTER 3

INSTRUMENT DESIGN

Introduction

The goal of this project was to construct a low cost, calibration free, and durable instrument that records reliable rain drop measurements. Previous designs have suffered from corrosion due to operation in harsh weather conditions. The corrosion would eventually damage an internal component that could not be repaired due to a design flaw that limited access to internal components. To address this issue, as well as others related to cost and reliability, a new prototype was built. The prototype of this instrument, shown in Figure 6, is an improved design of that originally designed by Michael Peter Cloos (Cloos, 2007). In the following chapter, the improved design, as well as the selection of materials and components used to construct the upgraded prototype, will be presented.



Figure 6 - The improved prototype.

Instrument Housing

One of the main criteria for the choice of materials for the instrument was that it must be able to endure harsh environments. The selection of materials used for the housing, which is the outer shell that protects the internal components, was as an important aspect of the design. Other criteria for the material included that it had to be easy to work, durable, and readily available. Additionally, the material had to have the capability of being constructed with water tight joints. Consequently, copper piping and Polyvinyl Chloride (PVC) piping were both tested as possible materials. The primary reason PVC was considered as an alternative material to copper was because it is less expensive and easy to work with. PVC was not rigid enough. Previous work had indicated that the flexing of the framework due to wind gusts would move the lasers in and out of optimal alignment, causing changes in the background signal levels. Therefore, copper was selected in order to prevent the instrument from vibrating or bending in the wind.

The laser head and detector head of the instrument were constructed out of 2 ½ inch

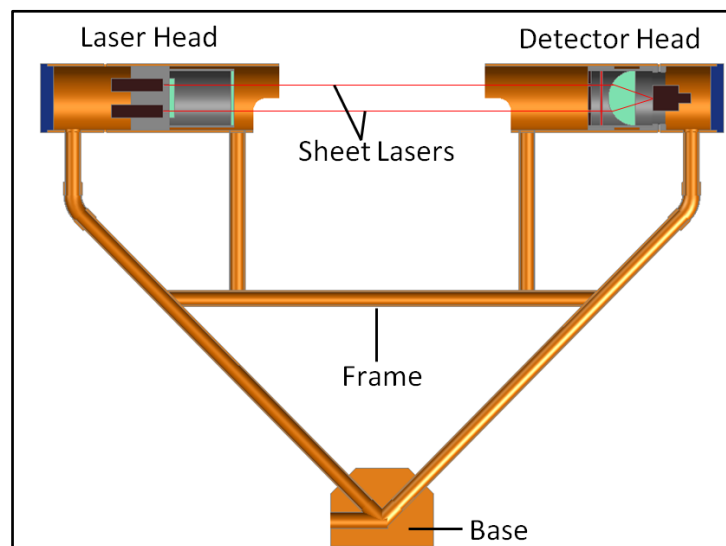


Figure 7 - The design of the housing constructed from copper. The laser head and detector head are made out of 2 ½ inch copper tubing. The frame is constructed from ½ inch copper tubing. The base is constructed from solid stock of 1 inch thick copper.

copper piping as shown in Figure 7. The outside ends of the heads are capped with Polystyrene caps machined to fit snugly and provide a watertight seal. The frame of the instrument was constructed out of ½ inch copper tubing. Lastly, the base was constructed from 1 inch solid stock copper. All of the copper joints were soldered together to prevent water from entering the interior of the instrument and to provide a rigid connection.

One improvement of the prototype compared to previous prototypes is the Polystyrene caps. Previous prototypes had copper caps soldered on the ends of the heads. The soldered on caps prohibited any adjustments or repairs that the electrical components or lenses may have needed inside the heads. In order to mitigate this problem, Polystyrene caps were machined to fit the ends of the copper tubing as shown in Figure 8. A thin coat of silicone is placed between the cap and copper tubing to ensure a water tight joint. The caps can be removed by breaking the silicone seal, allowing access to the internal components for adjustments and repairs.

Internal Components

Inside the laser head, two, 5 volt, 650 nm diode lasers are mounted vertically, separated by 1.187 cm as shown in Figure 8. The two laser beams pass through a cylindrical lens to expand

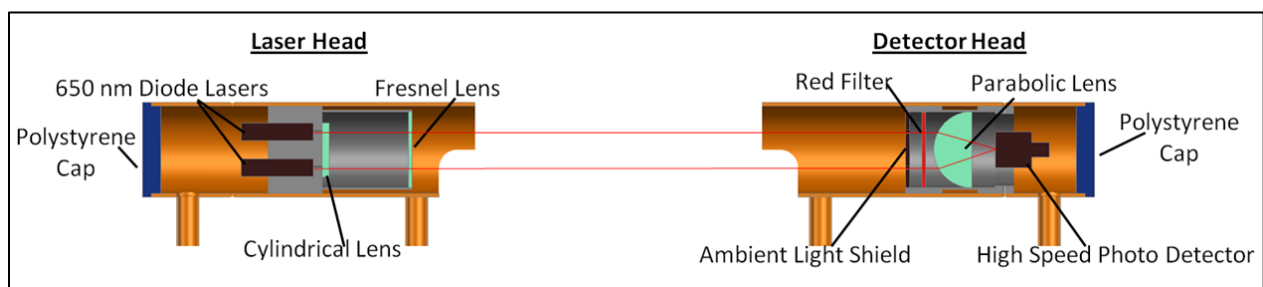


Figure 8 - The layout of the electrical and optical components located inside the laser head and detector head.

the beams in the lateral direction and a collimating lens that transforms the beams into two and half centimeter wide sheets. The cylindrical lens spreads the laser beams into laser sheets, while the collimating lens, in this case a Fresnel lens, redirects the two laser light sheets into a uniform laser sheet. This creates the sample area of the instrument.

Inside the detector head, each of the two laser sheets pass through an ambient light shield, a red filter, and a parabolic lens as shown in Figure 8. The ambient light shield is a cover with two slots for the lasers to pass through. Its purpose is to prevent ambient light from reaching the photo detector. Additionally, to help prevent ambient light from reaching the photo detector, a dichroic red filter was installed. The red filter blocks all ambient light except light with wavelengths of approximately 630 nm to 740 nm. The parabolic lens focuses both laser sheets to a single point on a high-speed silicon photo detector. The photo detector sends an analog signal to the computer, where voltage measurements are digitized at 66.6 kHz.

Cost of Instrument

One of the main design criteria for the instrument was cost. The total cost of the instrument excluding the computer and labor costs is \$ 873.48. Table 1 presents the individual costs associated with each component. Potential construction improvements to lower the cost even further such as selecting a less expensive material for the housing, or redesigning the structure of the frame to better accommodate the rigidity of PVC could be investigated.

Table 1- The itemized prices of the materials and components used to construct the instrument.

| | Quantity | Cost/item | Total Cost |
|------------------------------|----------|-----------|------------------|
| Housing | | | |
| 2.5 inch Copper Tubing | 2 feet | \$ 49.77 | \$ 49.77 |
| 0.5 inch Copper Tubing | 10 feet | \$ 18.05 | \$ 18.05 |
| 1 inch Copper Plate 6 X 6 | 1 | \$ 141.43 | \$ 141.43 |
| Polystyrene Rod | 1 | \$ 18.48 | \$ 18.48 |
| Optical Components | | | |
| Fresnel Lens | 1 | \$ 45.50 | \$ 45.50 |
| Cylindrical Lens Rod | 1 | \$ 45.00 | \$ 45.00 |
| Parabolic Lens | 1 | \$ 50.00 | \$ 50.00 |
| Dichroic Red Filter | 1 | \$ 37.50 | \$ 37.50 |
| Electrical Components | | | |
| 650 nm Diode Lasers | 2 | \$ 108.00 | \$ 216.00 |
| High Speed Photo Detector | 1 | \$ 130.00 | \$ 130.00 |
| Power Supply | 1 | \$ 121.75 | \$ 121.75 |
| Total Cost = | | | \$ 873.48 |

CHAPTER 4

DATA ANALYSIS

Introduction

As mentioned in Chapter 3, the ideal instrument should require no recalibration. Other disdrometers require frequent calibrations. The time it takes to calibrate instruments increases the operational cost associated with an instrument. Furthermore, if multiple instruments are used simultaneously to capture the spatial variability of a rainstorm the operational cost increases proportionately to the number of instruments. This new prototype requires no recalibration due to the design of the instrument and data analysis method. The following chapter will demonstrate how the velocity and diameter data is extracted from raw data using a new data analysis method.

Raw Data Acquisition

The measurement technique utilized to measure raindrops is an advantage of the instrument because it removes the need for recalibration. As a raindrop passes through the sampling area, it attenuates a portion of the laser light from reaching the photo detector. Two pulsed signals are produced as the droplet passes through the two laser sheets, as shown in

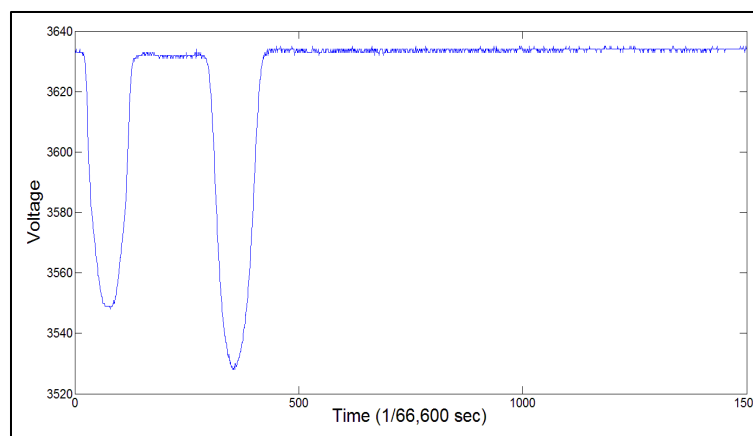


Figure 9 - A sample of raw data as a steel sphere passes through the sample area. The two pulsed signals correspond to the raindrop passing through and blocking the first laser sheet and second laser sheet, respectively.

Figure 9. The two pulsed signals correspond to the raindrop passing through and blocking the first laser sheet and second laser sheet, respectively.

If the hydrometeor is spherical and the laser sheet infinitely thin, the shape of the attenuated signal should be a cosine curve. However, it can be observed from Figure 10 that the individual pulsed signals do not fit a cosine function exactly as a steel sphere passes through the sample area. The primary reason the signal deviates from a cosine function is because the laser sheets have a finite thicknesses.

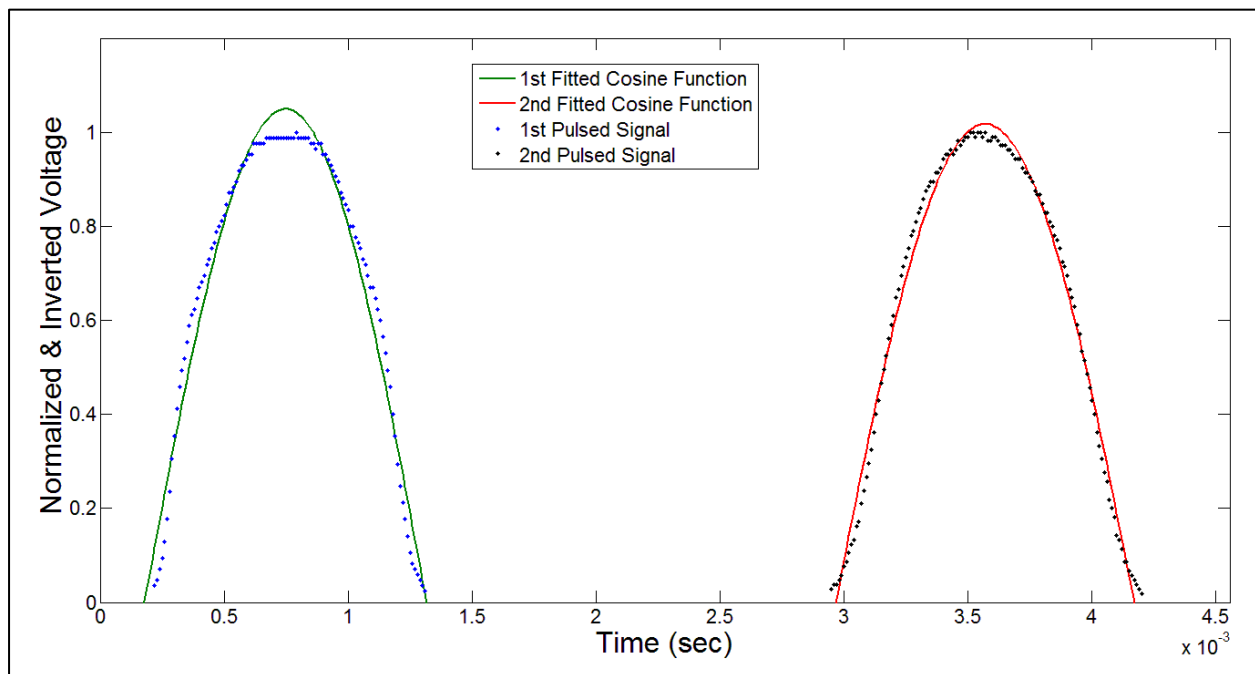


Figure 10 - Cosine functions fitted to the pulsed signals generated by a steel sphere. If the sheet lasers were infinitely thin the pulsed signals would fit the cosine curves.

The finite thickness of each laser sheet has two effects on the pulsed signal. The first effect is the peaks are flattened out as shown in Figure 11. The flat peaks are more distinct for hydrometeors smaller than the thickness of the laser sheets. The small hydrometeors block the maximum amount of laser light (i.e. they are completely illuminated) for a period of time as the hydrometeor is traveling, completely immersed, through the laser sheet. In contrast, for a large hydrometeor, the amount of light being blocked is changing with time continuously because the hydrometeor is larger than the thickness of the laser sheet as shown in Figure 12.

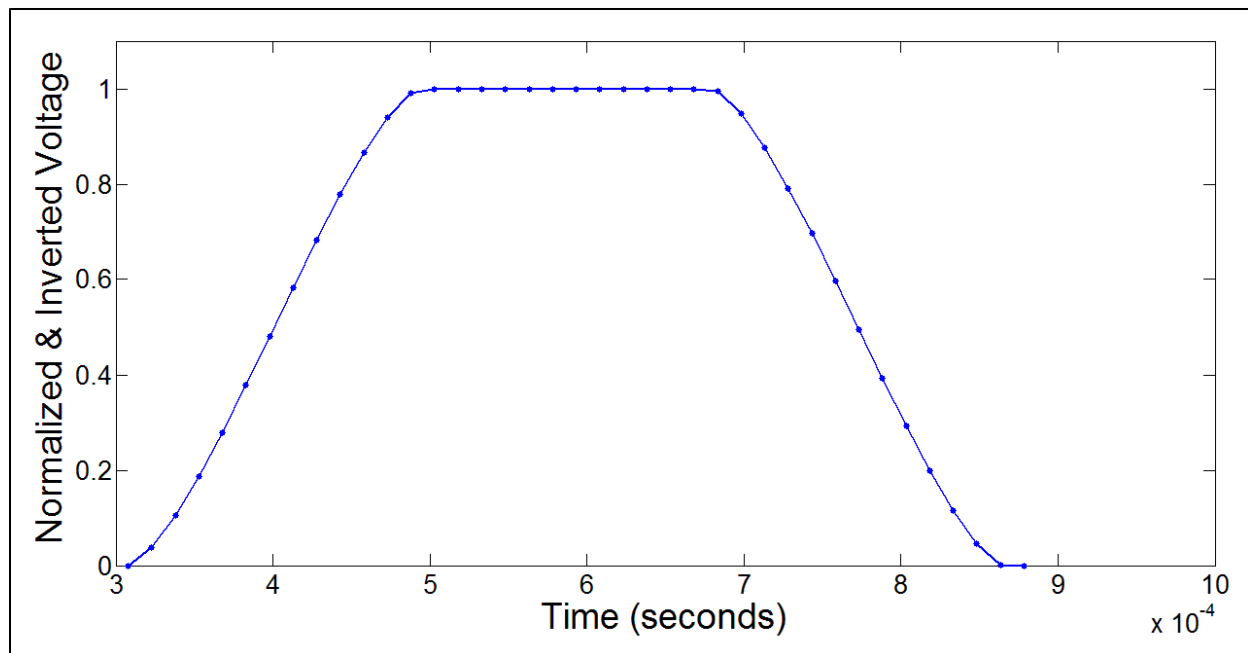


Figure 11 – An example of a pulsed signal produced by a sphere with a diameter smaller than the thickness of a laser sheet.

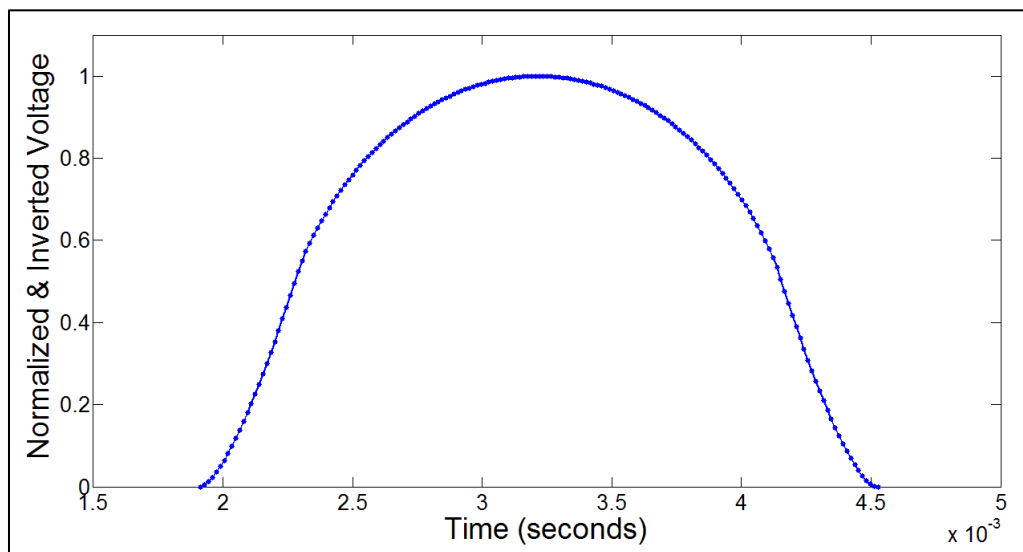


Figure 12 - An example of a pulsed signal produced by a spherical hydrometer larger than the thickness of the laser sheet.

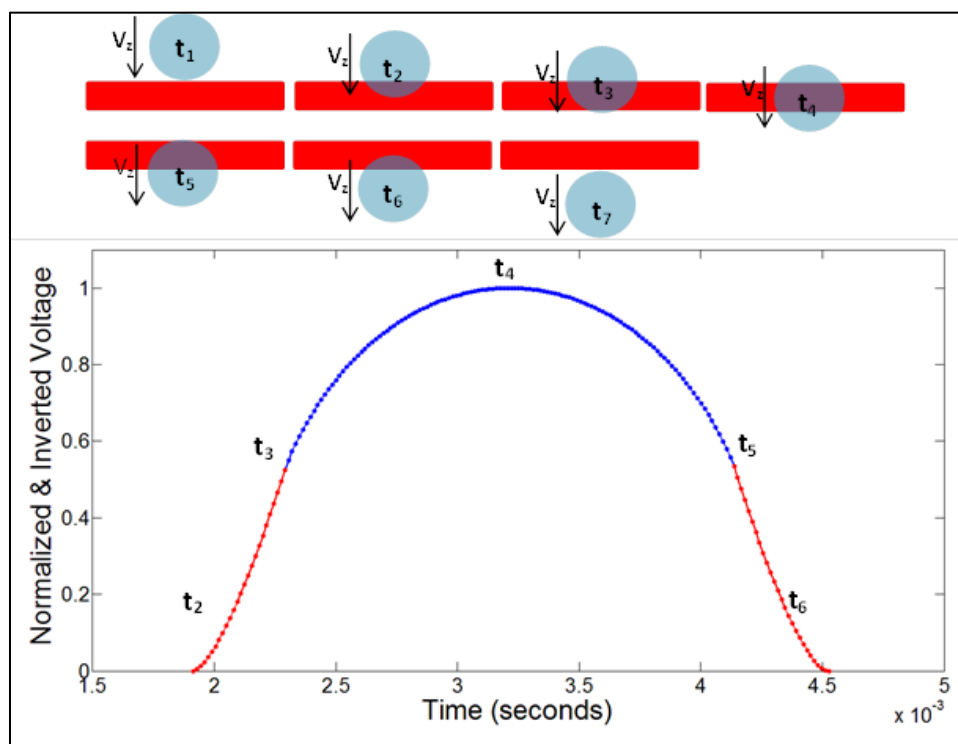


Figure 13 - An example of the tails produced by a spherical hydrometer passing through a laser sheet that has a thickness. The red portions of the signals are the tails.

The second effect is that the finite sheet thickness creates tails at the beginning and ending of each pulsed signal. These tails occur because it takes time for the hydrometeor to enter and exit the discrete thickness of the laser sheets as shown in Figure 13. The tails make it difficult to accurately estimate the beginning and ending of the pulsed signal.

Data Analysis

The lag time (t_{lag}) and time of attenuation (t_{att}) are two parameters obtained from the raw data shown in Figure 14. The lag time is the time between the peaks of the two pulsed signals. The lag time corresponds to the time it takes a hydrometeor to pass from the center of the top laser sheet to the center of the bottom laser sheet. The time of attenuation is the cumulative time it takes for a hydrometeor to pass through one laser sheet.

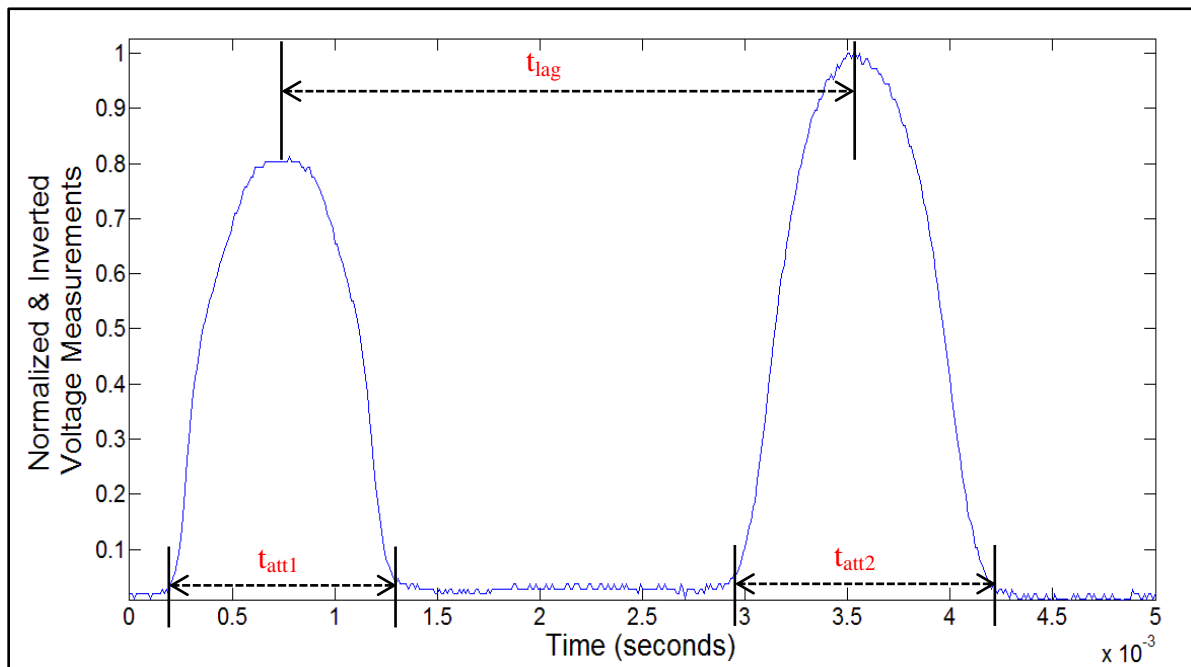


Figure 14 - An inverted and normalized data sample showing the parameters obtained from the raw data. The lag time (t_{lag}) is the time it takes the hydrometeor to travel from the center of one laser sheet to the center of the other. The time of attenuation (t_{att}) is the cumulative time it takes a hydrometeor to pass through one laser sheet. The time of attenuation can be measured twice from the two pulsed signals. t_{att1} corresponds to the first pulsed signal, and t_{att2} corresponds to the second pulsed signal.

Velocity Calculation

The velocity of the hydrometeors (V_z) is calculated by dividing the vertical distance between laser sheets by the lag time (t_{lag}) as seen in Equation 4.1.

$$V_z = \frac{d_L}{t_{lag}} \quad (4.1)$$

The distance between the sheet lasers (d_L) is a physical characteristic of the instrument and is constant throughout the sample area as long as the laser sheets are parallel. The distance between the laser sheets is 1.187 centimeters.

The flat peaks of the pulsed signals make determining the precise time at which a hydrometeor passes through the center of each laser sheet difficult. In order to estimate the time at which the peaks occur, a cosine function is fitted to each pulsed signal.

Theoretical Diameter Calculation

If the sheet lasers were infinitely thin, the diameter of the hydrometeor theoretically could be calculated using Equation 4.2, where V_z is the velocity of the hydrometeor obtained from Equation 4.1, and t_{att} is the time of attenuation extracted from the raw data.

$$D = t_{att} * V_z \quad (4.2)$$

Since the laser sheets have a discrete thickness, the time of attenuation has to be corrected. The time of attenuation (t_{att}) is estimated twice for each hydrometeor from the two pulsed signals. t_{att1} corresponds to the first pulsed signal and t_{att2} corresponds to the second pulsed signal. t_{att1} and t_{att2} are both overestimated because of the tails created from the sheet lasers having a thickness. If the sheet lasers were infinitely thin, the tails would not exist. To mitigate this overestimation, the tail time (t_{tail}) is subtracted from the time of attenuation (t_{att}). The tail time is the period of time it takes for the hydrometeor to travel the distance of the thickness of the laser as shown in Figure 13. The tail time is a function of the thickness of the sheet laser and the velocity of the hydrometeor. Therefore, the tail time is calculated using Equation 4.3 where h_L is the thickness of the sheet lasers, and V_z is the velocity of the hydrometeor.

$$t_{tail} = \frac{h_L}{V_Z} \quad (4.3)$$

Then Equation 4.4 is obtained by substituting Equation 4.1 for the velocity into Equation 4.3.

$$t_{tail} = \frac{h_L}{\left(\frac{d_L}{t_{lag}}\right)} \quad (4.4)$$

Then the corrected time of attenuation ($t_{corrected}$) is calculated, as shown in Equation 4.5.

$$t_{corrected} = t_{att} - t_{tail} \quad (4.5)$$

From the corrected time of attenuation ($t_{corrected}$) and the calculated velocity (V_Z), the diameter (D) can be calculated using Equation 4.6.

$$D = t_{corrected} * V_Z \quad (4.6)$$

Equation 4.7 is obtained by substituting Equation 4.1 into Equation 4.6.

$$D = t_{corrected} * \left(\frac{d_L}{t_{lag}}\right) \quad (4.7)$$

Substituting Equation 4.5 into Equation 4.7, Equation 4.8 is obtained.

$$D = (t_{att} - t_{tail}) * \left(\frac{d_L}{t_{lag}}\right) \quad (4.8)$$

Equation 4.9 is obtained by substituting Equation 4.4 into Equation 4.8 for t_{tail} .

$$D = \left(t_{att} - \frac{h_L}{\left(\frac{d_L}{t_{lag}}\right)}\right) * \left(\frac{d_L}{t_{lag}}\right) \quad (4.9)$$

Equation 4.10, the diameter data reduction equation, is obtained by simplifying Equation 4.9.

$$D = \frac{t_{att} * d_L}{t_{lag}} - h_L \quad (4.10)$$

The diameter of each hydrometeor could be calculated twice using parameters that correspond to the first and second pulsed signals. However, accurately determining the time of attenuation for each pulsed signal is difficult because there is not a distinct beginning and ending edge due to the background noise and the tails caused by the laser sheets having a thickness. In order to overcome this problem, a new method to calculate the diameter was used.

Half-Max Diameter Calculation

Two data reduction curves were developed for calculating the diameter from each pulsed signal. The data reduction curves are functions of the velocity and the time of attenuation at half the maximum of each pulsed. The half-max time of attenuation ($t_{1/2att}$) corresponds to the time duration for which the signal is greater than that at which half of the maximum attenuation occurs as shown in Figure 15. The time of attenuation at the half maximum was used because there is less uncertainty in determining the time of attenuation at half the max of the signal compared to the full time of attenuation.

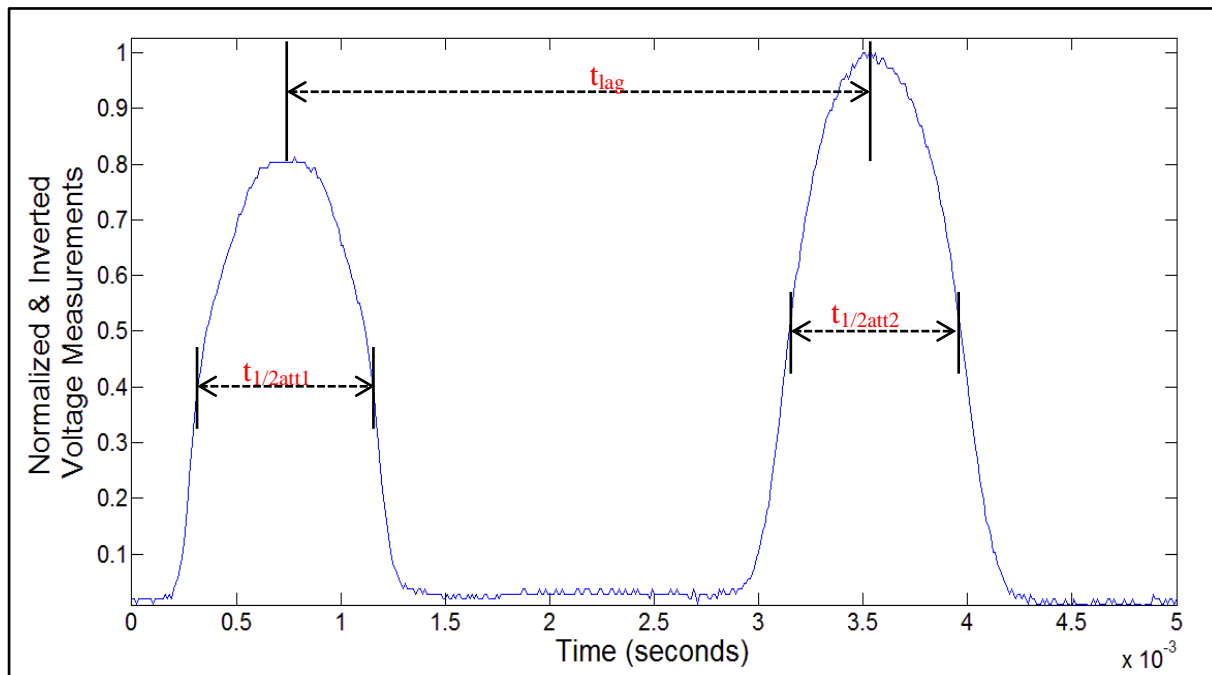


Figure 15 - An inverted and normalized data sample showing the parameters obtained from the raw data. The lag time (t_{lag}) is the time it takes the hydrometeor to travel past the two sheet lasers. The half max time of attenuation ($t_{1/2att}$) is the time between the half maximum of the signal. The half max time of attenuation can be measured two times from each pulsed signal. $t_{1/2att1}$ corresponds to the first pulsed signal, and $t_{1/2att2}$ corresponds to the second pulsed signal.

Two data reduction curves were developed. One curve from the first laser sheet and a second curve for the bottom laser sheet. The data reduction curves were developed by dropping fifty steel spheres of each diameter (0.98mm, 1.98mm, 2.98mm, 3.98mm, 4.98mm, and 5.98mm) through the sample area. The $\frac{1}{2}$ max diameters were calculated using Equations 4.11 and 4.12.

$$D1_{\frac{1}{2}max} = t_{\frac{1}{2}att1} * V_z \quad (4.11)$$

$$D2_{\frac{1}{2}max} = t_{\frac{1}{2}att2} * V_z \quad (4.12)$$

$D1_{\frac{1}{2}max}$ is the diameter calculated using the half max time of attenuation ($t_{1/2att1}$) from the first pulsed signal. $D2_{\frac{1}{2}max}$ is the diameter calculated using the half max time of attenuation ($t_{1/2att2}$) from the second pulsed signal. The half-max diameters were plotted against the actual size of the diameters in order to develop a data reduction curve. Using a second order polynomial and regression analysis the data reduction curve for each laser sheet was developed. Equations 4.13

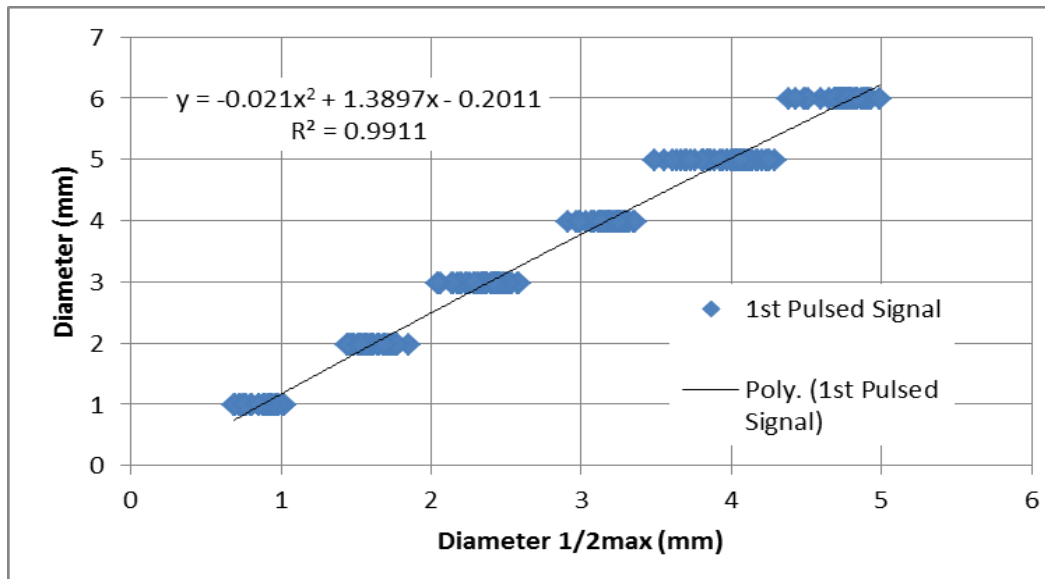


Figure 16 - 1st pulsed signal data reduction curve. The drop diameter is obtained by calculating the half-max diameter using the hydrometeors velocity and the half-max time of attenuation from the first pulsed signal $t_{1/2att1}$.

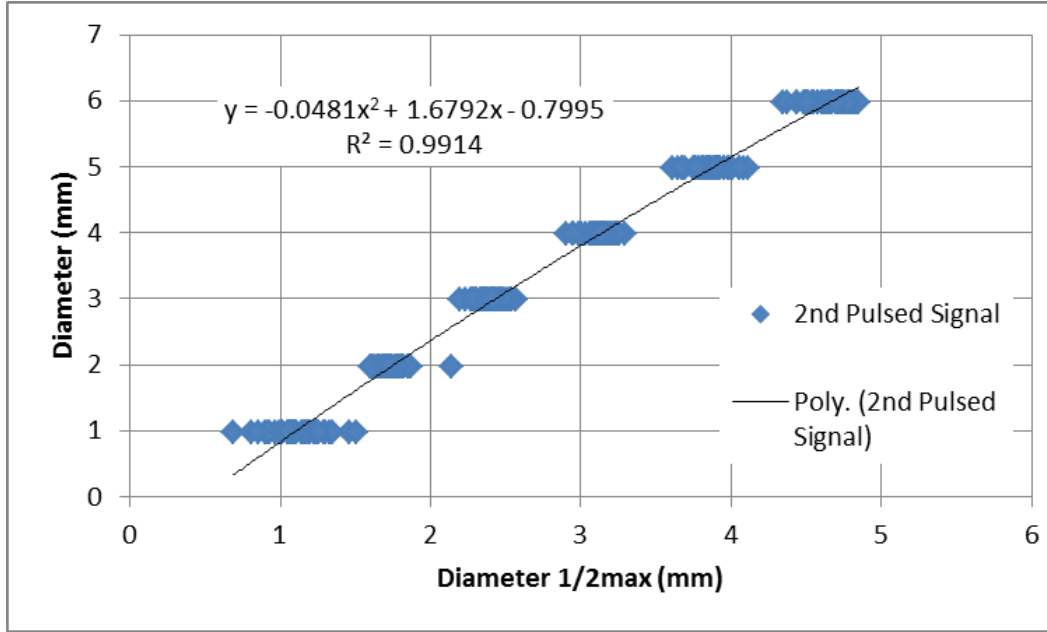


Figure 17 - 2nd pulsed signal data reduction curve. The drop diameter is obtained by calculating the half- max diameter using the hydrometeors velocity and the half-max time of attenuation from the second pulsed signal $t_{1/2att2}$.

and 4.14 are the two data reduction equations obtained from Figure 16 and Figure 17 where

$D_{1/2max}$ corresponds to first pulsed signal and $D_{2/2max}$ corresponds to the second pulsed signal.

$$D_{1corrected} = -0.021 * D_{1/2max}^2 + 1.3897 * D_{1/2max} - 0.2011 \quad (4.13)$$

$$D_{2corrected} = -0.0481 * D_{2/2max}^2 + 1.6792 * D_{2/2max} - 0.7995 \quad (4.14)$$

The data reduction curves are then used to determine the diameters of hydrometeors sampled by the instrument. $D_{1corrected}$ and $D_{2corrected}$ are averaged together to determine the final diameter (D_F) as shown in Equation 4.15.

$$D_F = \frac{D_{1corrected} + D_{2corrected}}{2} \quad (4.15)$$

Limitation of Half-Max Diameter Calculations

The half-max data reduction method has a lower limit at which hydrometeors can be measured. A hydrometeor that has a radius equal to or less than the thickness of the laser sheets cannot be estimated using the half-max diameter method. For a drop radius equal to or less than the thickness of the laser sheets this method returns the same $D_{1/2max}$. The same $D_{1/2max}$ is returned because the half-max time of attenuation is the time between when the leading half of the hydrometeor is immersed in the laser sheet, and the time when the trailing half is immersed in the laser sheet. This corresponds to the time it takes the center of the hydrometeor to travel the thickness of the laser sheet. Therefore, Equation 4.11 and 4.12 return the thickness of the laser sheets for this case. The thicknesses of the top and bottom laser sheets are approximately 0.45

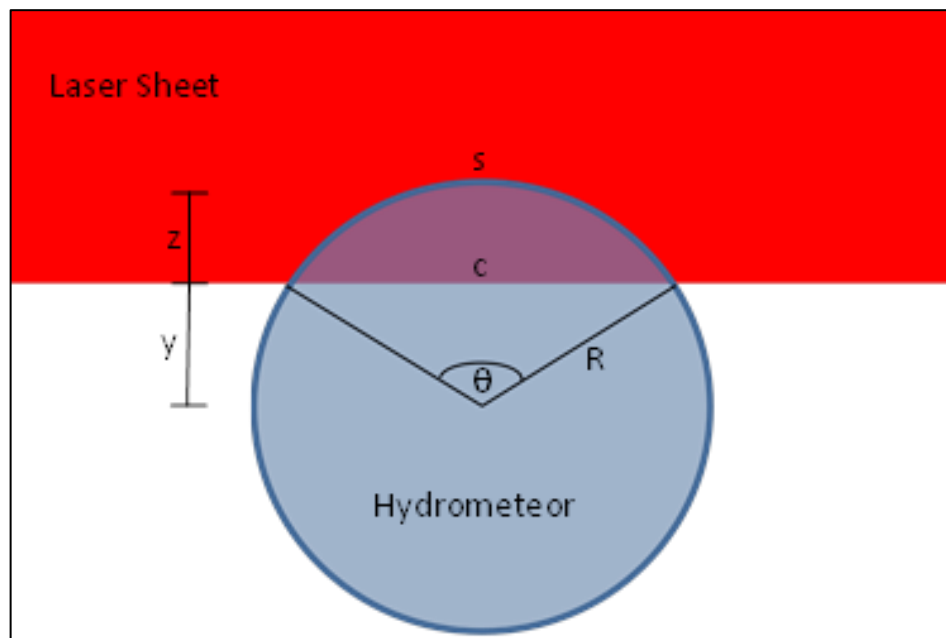


Figure 18 - Schematic of a drop with a radius smaller than or equal to the laser sheet thickness exiting the laser sheet. The amount of light being attenuated corresponds to the projected area remaining in the laser sheet.

mm and 0.65mm, respectively. Therefore the smallest diameters that can be estimated are 0.90 mm and 1.3 mm using the first and second pulsed signals.

In an attempt to estimate the small hydrometeors that are equal to or smaller than 0.90 mm a relationship was developed to model amount of laser light being attenuated by these hydrometeors. The relationship models a hydrometeor from the time the center of the hydrometeor exits the laser sheet to the time the trailing edge exits the laser sheet. At the time when the trailing half of the hydrometeor is immersed in laser light, the pulsed signal is at half-max. Using this as a reference point, the amount of laser light being attenuated (K) can be calculated for any time thereafter using Equation 4.16 where y is the distance from the center of the hydrometeor to the bottom edge of the laser sheet as shown in Figure 18. The amount of laser

$$K = a \left[R^2 * \cos^{-1} \left(\frac{y}{R} \right) - y * \sqrt{R^2 - y^2} \right] \quad (4.16)$$

light being attenuated is the sector of the projected area remaining in the laser sheet. y can be calculated using Equation 4.17.

$$y = \Delta t * V_z \quad (4.17)$$

R is the radius of the hydrometeor. Δt is the change in time from the time after the center has exited the laser sheet. a is a coefficient that is found by solving Equation 4.16 using the reference point at the half-max. Equation 4.18 was calculated by substituting Equation 4.17 into 4.16.

$$K = a \left[R^2 * \cos^{-1} \left(\frac{\Delta t * V_z}{R} \right) - \Delta t * V * \sqrt{R^2 - (\Delta t * V_z)^2} \right] \quad (4.18)$$

The model does not account for the variation of energy density across the thickness of the laser sheets. The energy density in the center of the thickness of the laser sheet will be the greatest, and the edges of the laser sheet will be the smallest. The variations in the energy densities would also influence the amount of laser light energy being attenuated.

To calculate hydrometeors with radii smaller than the thickness of the laser sheets, Equation 4.18 was fitted to the ending edges of each pulsed signal by varying the radius in order to minimize the sum of the differences squared between Equation 4.18 and the pulsed signals as shown in Figure 19. As mentioned previously, the half maximum was used as the reference.

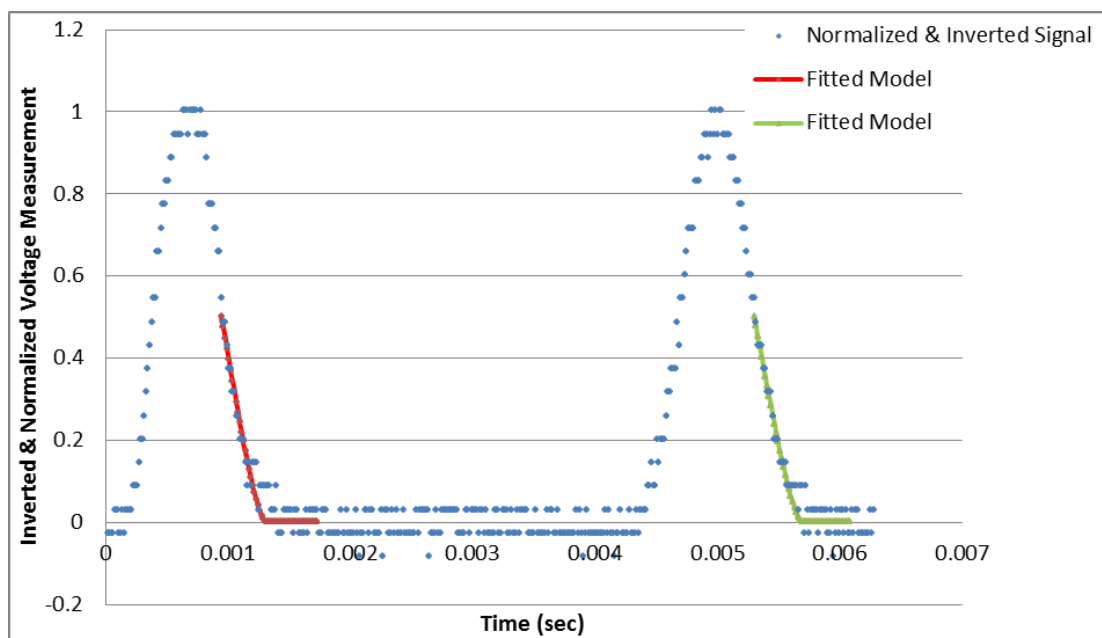


Figure 19 - A model fitted to the two pulsed signals used to estimate the radius produced by a hydrometeor with a radius equal to or smaller than the laser sheet thicknesses.

While analyzing these small drops using this method, it was discovered that signals produced from spheres less than 1 mm took the shape of stair steps as shown in Figure 20. The pulsed signals become stair steps because the instrument has a finite number of digitizing channels and the small changes from small drops entering and exiting the laser sheet are not large enough to be detected. Therefore, fitting Equation 4.18 produced inaccurate results because of the stair step shape and the small number of data points to fit the data to. In order to use this analysis method effectively, the resolution of the instrument must be increased.

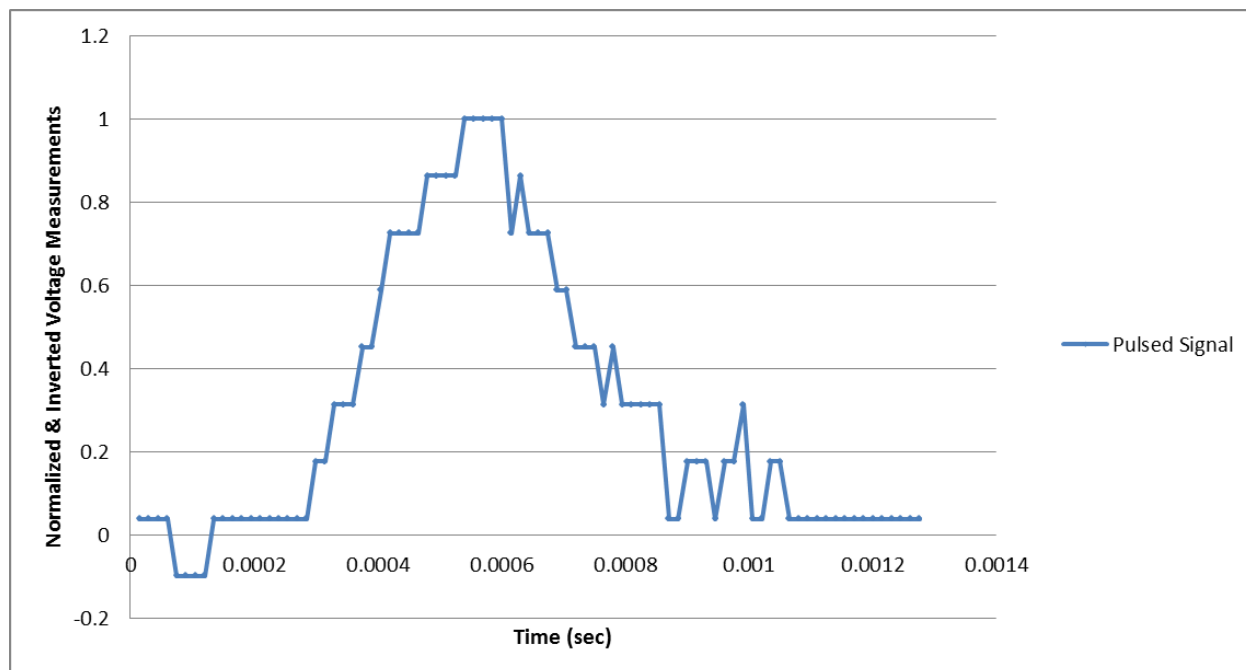


Figure 20 - An example of a stair step signal produced by a small hydrometer.

CHAPTER 5 INSTRUMENT VALIDATION

Introduction

After the instrument was built, two lab experiments were performed to test the accuracy and precision of the instrument. The first experiment consisted of dropping steel spheres with a range of diameters through the sample area. The second experiment consisted passing a known volume of water through the sample area in the form of droplets. This chapter will describe the experiments in detail.

Steel Sphere Experiment

The purpose of the Steel Sphere Experiment was to assess the accuracy and precision of the measured velocity and diameter made by the prototype. Steel spheres were used to simulate hydrometeors falling through the sample area. Steel spheres were selected because their shape was well defined, and their diameters were accurately known. Steel spheres with diameters of 0.98mm, 1.98 mm, 2.98mm, 3.98 mm, 4.98 mm and 5.98 mm were each dropped through the sampling area one hundred and fifty times using a mechanical device developed by Renato Frasson to test disdrometers. The device drops spheres from a fixed height, with no initial vertical velocity in a repeatable manner. The experimental setup is shown in Figure 21.

The measured diameters were compared against the diameters measured using calipers with a 0.01mm resolution. The velocities measured by the prototype were compared against the kinematic equation for an object falling from a known height as shown in Equation 5.1.

$$V_f = V_i + \sqrt{2gh} = 0\text{m/s} + \sqrt{2 * \left(\frac{9.81\text{m}}{\text{s}^2}\right) * 0.396\text{m}} = 2.79\text{m/s} \quad (5.1)$$

V_f is the velocity at height h . V_i , the initial velocity, is zero since the steel spheres are starting from rest. g is acceleration due to gravity. h is the height from which the steel spheres were dropped. h was 0.396 meters in this experiment. The drag force acting on the spheres was assumed zero due to the short drop height and small frontal areas of the spheres.



Figure 21 – Steel Sphere Experimental Setup. The steel spheres were dropped from a height of 0.396 meters.

Steel Sphere Experiment Results

The resulting velocities for each diameter size tested are shown in Table 2 and the resulting diameters are shown in Table 3.

Table 2 -The resulting velocities for each diameter tested.

| Sphere Diameter mm | Averaged Measured Velocity m/s | Standard Deviation m/s | Average Fractional Error % | Average Error % |
|-------------------------------------|-------------------------------------------------|-----------------------------------------|---------------------------------------------|----------------------------------|
| 0.98 | 2.697 | 0.018 | 0.66 | -3.33 |
| 1.98 | 2.756 | 0.018 | 0.64 | -1.24 |
| 2.98 | 2.768 | 0.018 | 0.66 | -0.79 |
| 3.98 | 2.773 | 0.016 | 0.58 | -0.60 |
| 4.98 | 2.782 | 0.020 | 0.74 | -0.27 |
| 5.98 | 2.761 | 0.023 | 0.84 | -1.03 |

Table 3 - The resulting diameters for each diameter tested.

| Sphere Diameter mm | Average Measured Diameter mm | Standard Deviation mm | Average Error mm | Average Fractional Error % |
|-----------------------|------------------------------------|-----------------------------|------------------------|----------------------------------|
| 0.98 | 1.044 | 0.124 | 0.06 | 12.63 |
| 1.98 | 1.987 | 0.091 | 0.01 | 4.62 |
| 2.98 | 2.969 | 0.081 | -0.01 | 2.73 |
| 3.98 | 3.976 | 0.098 | 0.00 | 2.47 |
| 4.98 | 4.993 | 0.113 | 0.01 | 2.28 |
| 5.98 | 5.933 | 0.113 | -0.05 | 1.89 |

A comparison of the average fractional errors corresponding to each diameter size tested is shown in Figure 22.

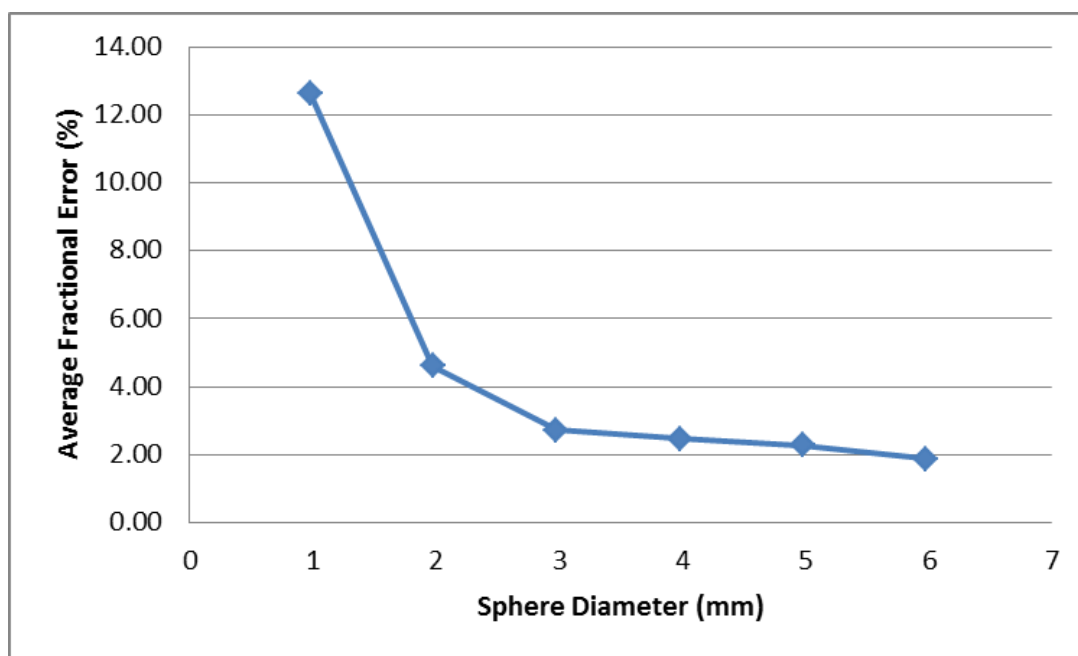


Figure 22 - The average fractional errors associated with each diameter tested. The average fractional error decreases with increasing diameters.

Steel Sphere Experiment Discussion

The average estimated velocity of the 150 trials for each sphere diameter tested was smaller than the calculated theoretical velocity of 2.79 meters per second. The largest average bias error, -3.33 percent, was associated with the 0.98 mm sphere trials. The 0.98mm sphere trials had the largest average bias error because the spheres were dropped by hand from a lower height of 0.371 meters. The device used to drop the spheres did not work for the 0.98 mm spheres because the spheres would get jammed in the device. The average estimated velocities from the other diameters tested had average bias errors between -1.24 percent and zero. Not accounting for the drag force acting on the spheres is one reason why all the average velocities are slightly lower than the calculated theoretical velocity. Also, the accuracy of determining the distance between the laser sheets, d_L , is another reason that could contribute to the consistent uncertainty of the average measured velocities. The brightness of the laser sheet and thickness of the laser sheet make it difficult to determine the exact centers of the laser sheets. d_L was measured to be 11.87 millimeters \pm 0.05 millimeters. Lastly, any error in measuring the height from which the spheres were dropped could contribute to a consistent difference between the measured and theoretical velocities.

The standard deviation of the measured velocities for each diameter size tested was equal to or less than 0.023 meters per second. The average fractional error of the averaged measured velocities ranged from 0.58 to 0.84 percent for each diameter tested. As a comparison the theoretical average fractional error was estimated to be 0.005 or 0.5 percent using Equation 5.2.

$$\frac{\delta V_z}{V_z} = \left(\left(\frac{\delta t_{lag}}{t_{lag}} \right)^2 + \left(\frac{\delta d_L}{d_L} \right)^2 \right)^{\frac{1}{2}} \quad (5.2)$$

d_L was 11.87mm. The estimated precision of the distance between the laser sheets, δd_L , was 0.05 millimeters. A typical t_{lag} of 0.0043 seconds from this experiment was used. δt_{lag} is the precision with which the time when the center of the steel sphere passes through each laser sheet (i.e. the time between the peaks of the pulsed signals) can be determined. The theoretical precision of t_{lag} was determined to be $\pm 1.06 \times 10^{-5}$ seconds using Equation 5.3, where δt_1 and δt_2 describe the

$$\delta t_{lag} = \sqrt{(\delta t_2)^2 + (\delta t_1)^2} \quad (5.3)$$

precision of determining the times when the two peaks from the pulsed signals occur. δt_1 and δt_2 are estimated to be 7.5×10^{-6} seconds, half the temporal resolution of the new prototype.

The theoretical estimated fractional error of a velocity measurement is slightly lower than the measured fractional errors of the velocities. One reason for this is because the flat peaks of the pulsed signals make it difficult to determine the exact time at which the center of the steel sphere passes through the center of each laser sheet. To increase the precision of determining the time when the peaks occur, a cosine curve was fit to each signal.

The measured average fractional error of the measured diameters decreases with increasing diameter size as shown in Figure 22. This makes sense since the error, estimated by the standard deviations of the diameters tested, were all approximately 0.1 mm. Thus, the standard deviation is a larger fraction of the diameters for smaller spheres compared to larger spheres.

The measurements of the diameter depend on the velocity and the half-max time of attenuation ($t_{att1/2max}$) of the pulsed signals. The theoretical fractional error of the diameter measurements associated with a 0.98mm sphere and 5.98 mm sphere was estimated using Equation 5.4.

$$\frac{\delta D}{D} = \left(\left(\frac{\delta V_z}{V_z} \right)^2 + \left(\frac{\delta t_{att1/2max}}{t_{att1/2max}} \right)^2 \right)^{\frac{1}{2}} \quad (5.4)$$

The previous estimated theoretical fractional error of a velocity measurement, 0.005, was used in this analysis. $\delta t_{att1/2max}$ was assumed to have the same precision as the lag time, 1.06×10^{-5} seconds, since both parameters are functions of the difference of two times measured by the same computer timer. The fractional error associated with the data reduction curves was not included when determining the theoretical fractional error of the diameter measurements. The theoretical fractional error for a 0.98mm sphere was estimated to be 0.03 or 3 percent and for a 5.98mm sphere, 0.0079 or 0.79 percent. The measured diameter fractional errors are much

greater than the estimated theoretical fractional errors. One reason for this is that determining the exact half-max time of attenuation is made more difficult by the signal to noise ratio.

Additionally the signal to noise ratio increases for smaller drops further increasing the error of determining the half-max.

Drip Experiment

To further study the performance of the instrument, a drip experiment was performed in the lab. This experiment was developed to simulate hydrometeors more realistically. The drip experiment consisted of dropping water droplets through the sample area of the new prototype. The water droplets were dropped using an apparatus similar to those used during titrations of chemicals. One trial consisted of dropping 25 mL of water, in the form of water droplets, through the sample area. The water droplets were dropped from 0.91 meters above the sample area of the instrument. 22 trials were performed. The Drip Experiment setup is shown in Figure 23.

The cumulative volume of water (Ψ) that passed through the sampling area of the instrument for each trial was calculated using Equation 5.5, where D is the diameter of the water droplet.

$$\Psi = \sum_i^n \frac{\pi D_i^3}{6} \quad (5.5)$$

The cumulative volume calculated for each trial was compared against the 25 mL released from the pipet.

Drip Experiment Results

The individual results for each of the 22 trials recorded during the Drip Experiment are shown in Figure 24. The average measured volumes recorded during the Drip Experiment are shown in Table 4.

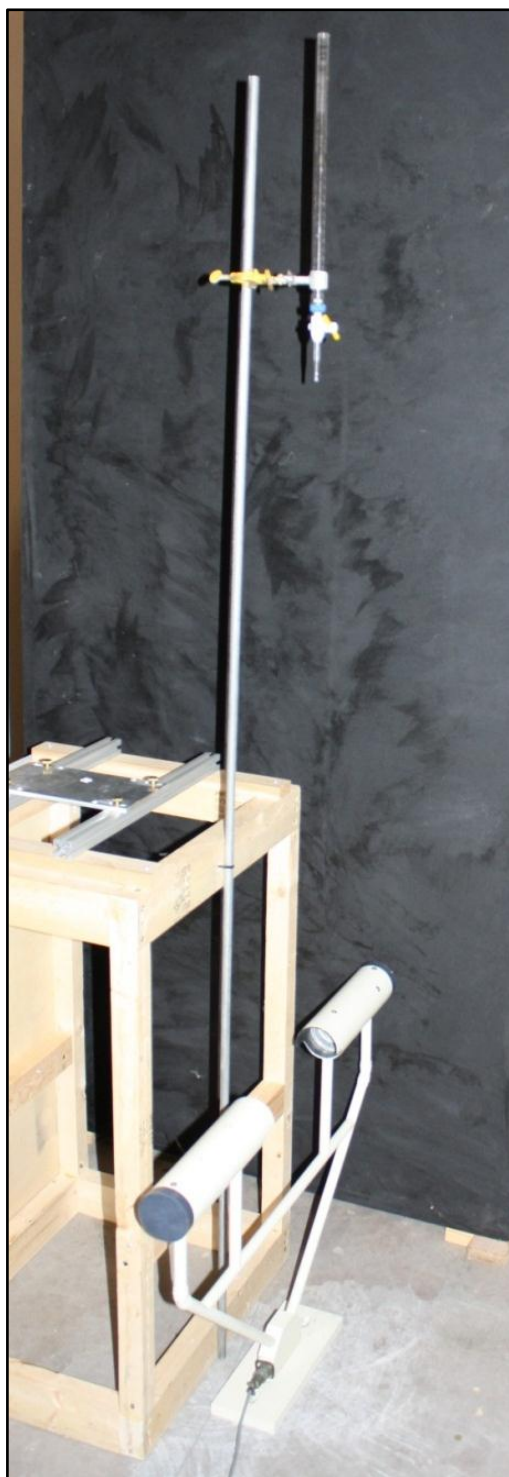


Figure 23 - Drip Experiment Setup

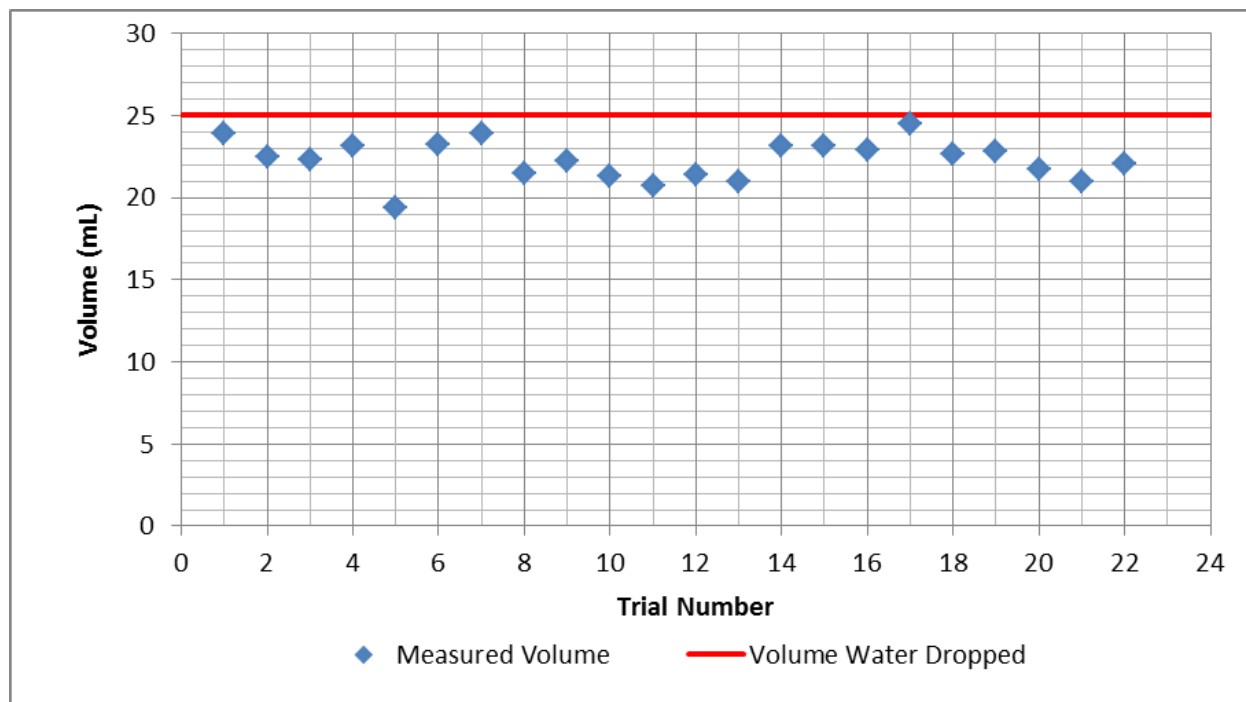


Figure 24 - Results of the 22 trials recorded during the drip experiment.

Table 4 - Average results from Drip Experiment.

| | Measured Volume (mL) | Error (mL) | % Error | # Drops Analyzed |
|---------------------------|----------------------|------------|---------|------------------|
| Average | 22.30 | -2.70 | 10.79 | 476 |
| Standard Deviation | 1.18 | 1.18 | 4.74 | 35 |

Drip Experiment Discussion

All of the trials underestimated the actual volume of water released through the sample area. The average measured volume of the twenty two trials was 22.30 mL with a standard deviation of 1.18 mL. Errors acquired while measuring the diameter are magnified by a factor of three times when calculating the volume of a water droplet. Furthermore, errors associated with individual drops accumulate when summing up the total volume of the drops that passed through

the sample area for each trial. However, even with the volume estimates being sensitive to errors, the average percent error was only 10.79 percent. Therefore, it was estimated that the average percent error per drop is 2.3 percent using Equation 5.6.

$$\text{Average \% Error per drop} = \frac{\text{Average \% Error}}{\text{Average \# Drops}} \quad (5.6)$$

Conclusions of Lab Experiments

Two lab experiments were performed to assess the accuracy and precision of the new prototype. The first experiment consisted of dropping 150 steel spheres with the same diameter through the sample area from the same height. The diameters tested were 0.98 mm, 1.98mm, 2.98mm, 3.98mm, 4.98mm, and 5.98mm. The average measured fractional percent errors of the velocity measurements were all less than 1 percent. The average bias errors of the velocities compared to the theoretical velocity ranged from -3.3 to -0.27 percent for the diameters tested. The 0.98mm had the largest average error of -3.3 percent because the device used to release the spheres did not work for this size sphere. Thus the spheres were dropped by hand from a slightly lower height. The consistent underestimation of the average velocities compared to the theoretical velocity was expected since the drag force was not accounted for when calculating the theoretical velocity.

The average measured fractional percent error of the diameter measurements decreased with increasing diameter size. This trend was consistent with what was expected since the standard deviation for each diameter tested was approximately 0.1 mm. The magnitude of the fractional errors ranged from 12.4 percent for the 0.98 mm diameters to 1.79 percent for the 5.98mm diameters. The majority of the fractional error occurs when determining the half-max time of attenuation because of the signal to noise ratio. Also, for smaller drops, the signal to noise ratio increases which increases the error in determining half-max time of attenuation.

The second experiment performed was the Drip Experiment. The Drip Experiment consisted of dropping 25 mL of water through the sample area in the form of droplets. The

average volume measured was 22.30 mL with a standard deviation of 1.18 mL. The average error was 10.79 percent. The average error was accumulated over an average of 476 drops per trial. Considering the errors associated with the diameter estimates are magnified and accumulated over the total number of drops analyzed, the average error is reasonable.

CHAPTER 6 OUTDOOR TESTING

Instrument Location

The new prototype was placed outside on the roof of The University of Iowa Hydraulics East Annex in Iowa City as shown in Figure 25 from February 20th to March 13th, 2012. This location was secure and provided easy access to the instrument in case the instrument needed to be adjusted or repaired.

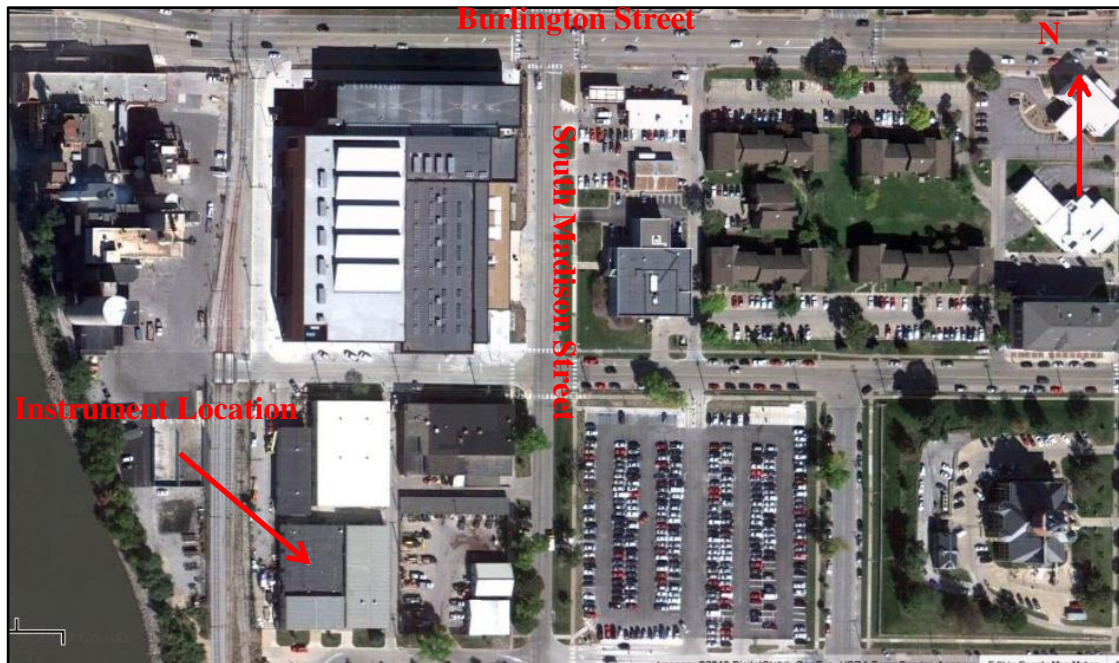


Figure 25 – A map showing the location where the new prototype was placed outside to record precipitation events.

Additionally, an Iowa Flood Center Tipping Bucket was located on the roof of The University of Iowa Hydraulics Annex. The data collected from the tipping bucket was compared against the data collected by the new prototype.

Data Sets

During the time the new prototype was placed outside, three precipitation events were recorded. The first precipitation event was in the form of rain, and it occurred from 0:00 to 2:00 hours on February 29th, 2012. According to www.weatherunderground.com the rain event was characterized as a thunderstorm with heavy rain. The drop size distribution DSD is shown in Figure 26.

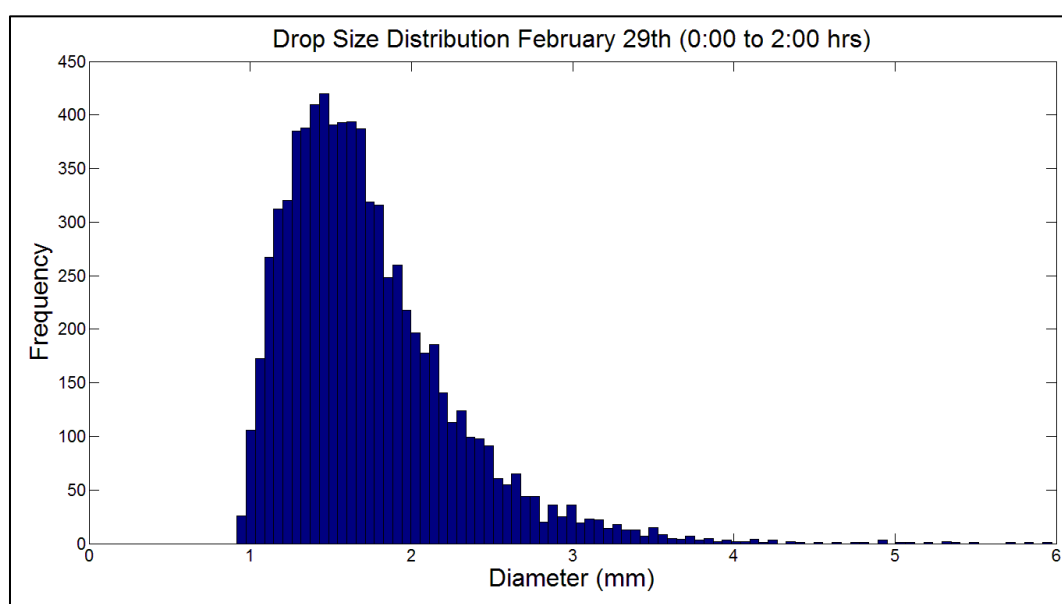


Figure 26 - The drop size distribution recorded during a thunderstorm on February 29th.

Later on February 29th, 2012, between the hours of 14:00 and 17:00 the instrument recorded a snow event. It should be noted that the relationship between the snowflakes and their size has not been investigated. Therefore the reported sizes should be valued with zero confidence. However, it is worthy to note that the instrument is capable of measuring snowflakes as shown in Figure 27.

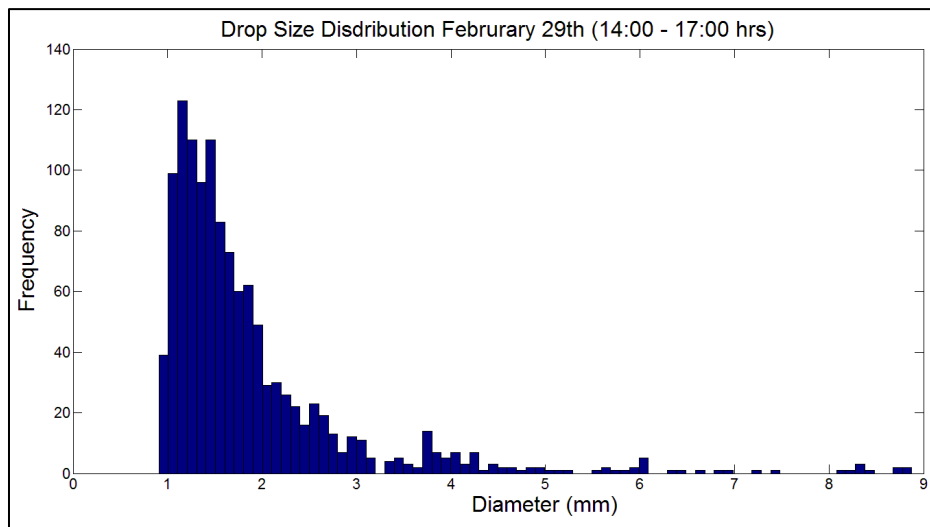


Figure 27 - A snow event captured on February 29th (14:00 - 17:00hrs). The size of the snowflakes has not been studied and therefore should not be valued with any confidence.

Lastly, on March 12th, 2012, the instrument recorded a rain event from 8:00 to 10:45. The rain event was characterized as light rain according to www.weatherunderground.com. The DSD for this time period is shown in Figure 28

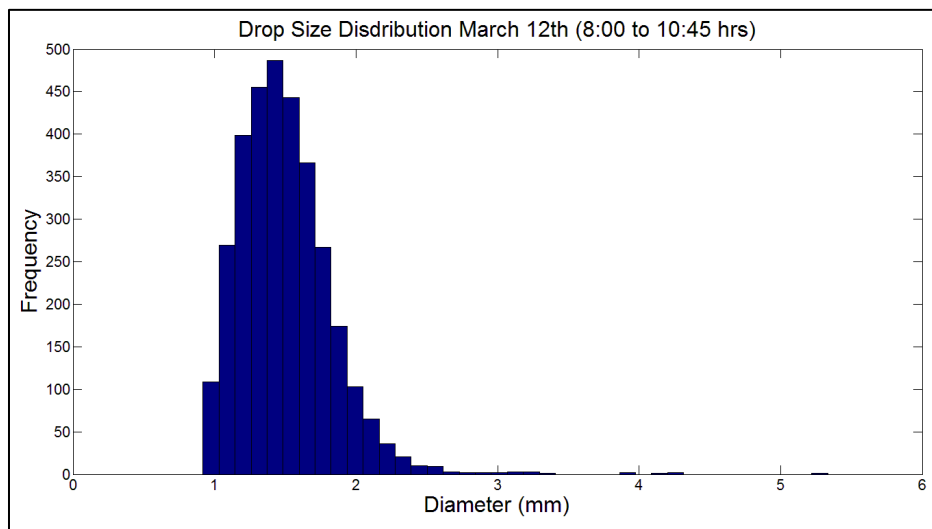


Figure 28 - The DSD from a light rain on March 12th.

Instrument Comparison

The rain rate (RR) captured by the new prototype and the tipping bucket were compared against each other. The rain rate determined from the DSD captured by the new prototype was calculated using Equation 6.1.

$$RR\left(\frac{mm}{10-min}\right) = \frac{1}{\Delta T * SA} \sum_{i=1}^n \frac{\pi D_i^3}{6} \quad (6.1)$$

ΔT is the averaging time which was ten minutes in this analysis. SA is the sample area, which was measured to be 88 centimeters squared. n is the number of drops which were measured during the averaging time and D_i is the diameter of the ith drop.

The tipping bucket measures the volume of water by counting the number of times the bucket tips. One bucket tip corresponds to one-one hundredth of an inch or 0.254 millimeters of water. Therefore, the rain rate is calculated by summing the number of bucket tips over the averaging time. The rain rates for February 29th and March 12th are shown in Figure 29 and Figure 30. Another comparison of the instruments is shown in Figure 31.

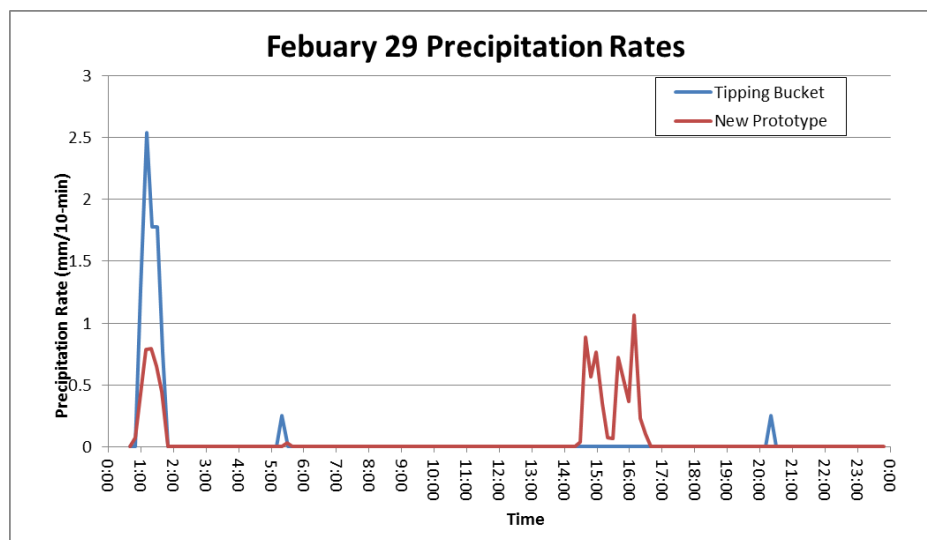


Figure 29 - A comparison of Precipitation Rates between a tipping bucket and the new prototype. It thunder stormed between 0:00 and 2:00 hours and it snowed between 14:00 and 17:00 hours.

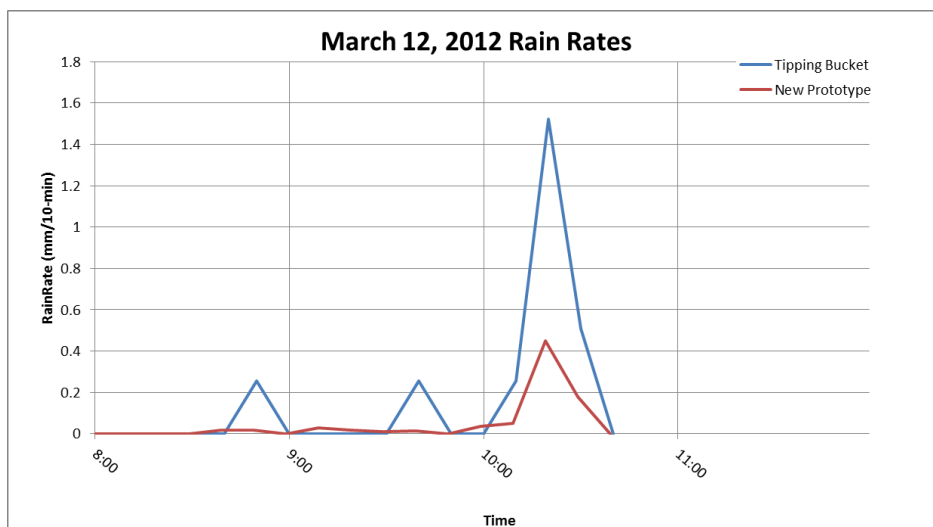


Figure 30 – The rain rates measured by the new prototype and tipping bucket on March 12th, 2012. The rain event was categorized as light rain.

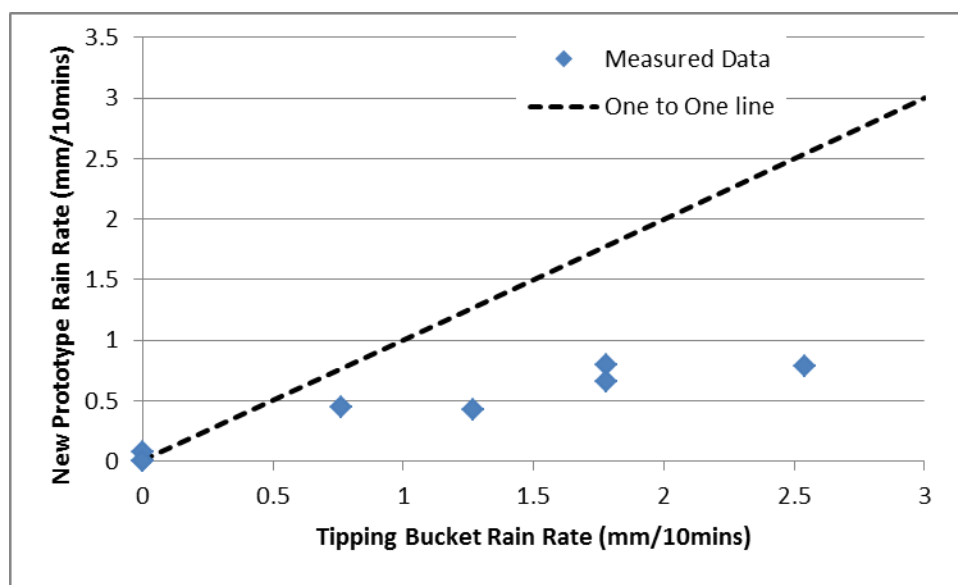


Figure 31 - A comparison of the measured rain rates captured by the prototype and tipping bucket during the rain event on February 29th, 2012. The instruments are in better agreement at lower rain rates.

Velocity

The new prototype measures the velocity and diameter of hydrometeors. Gunn and Kinzer performed lab experiments to obtain benchmark data for the relationship between drop diameter and terminal velocity (Gunn & Kinzer, 1949). The measured data for each precipitation event was compared against the Gunn and Kinzer Relationship as shown in Figure 32, Figure 33, and Figure 34.

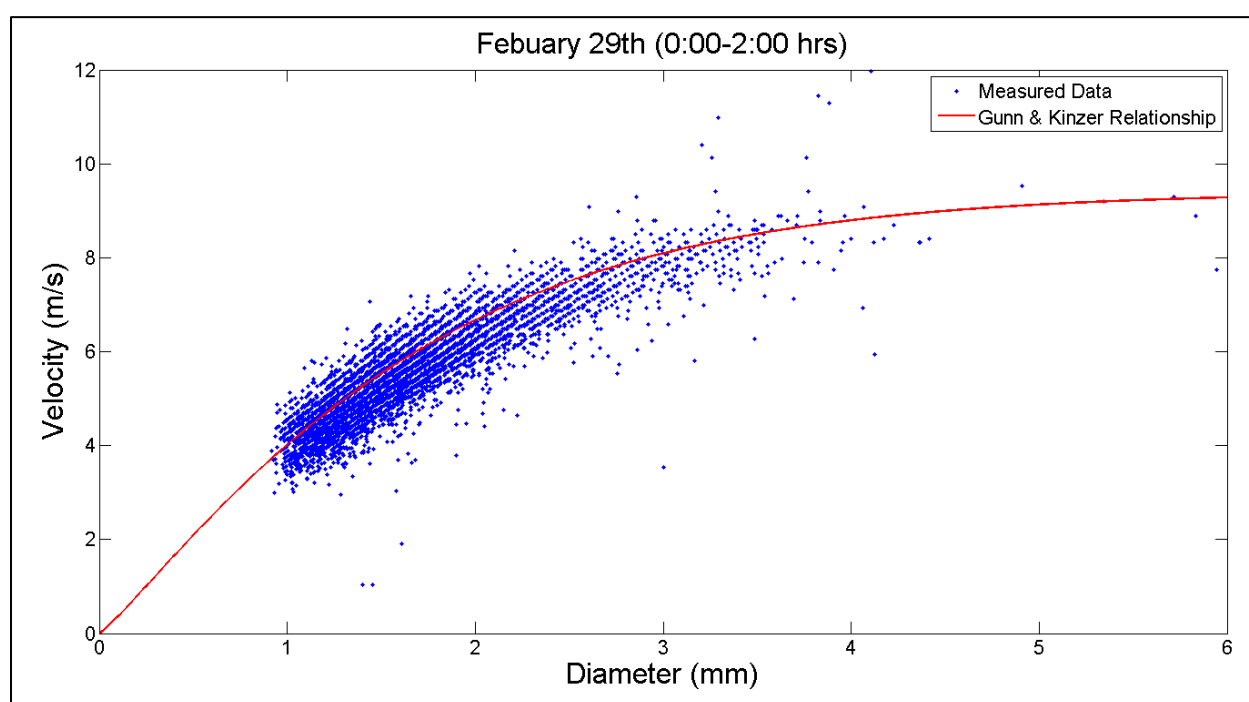


Figure 32 - A comparison of the measured velocities during a thunderstorm captured on February 29th, 2012 against the theoretical Gunn and Kinzer Relationship. The scatter of the measured data is mostly likely due to the dynamic environment in which the measurements were taken.

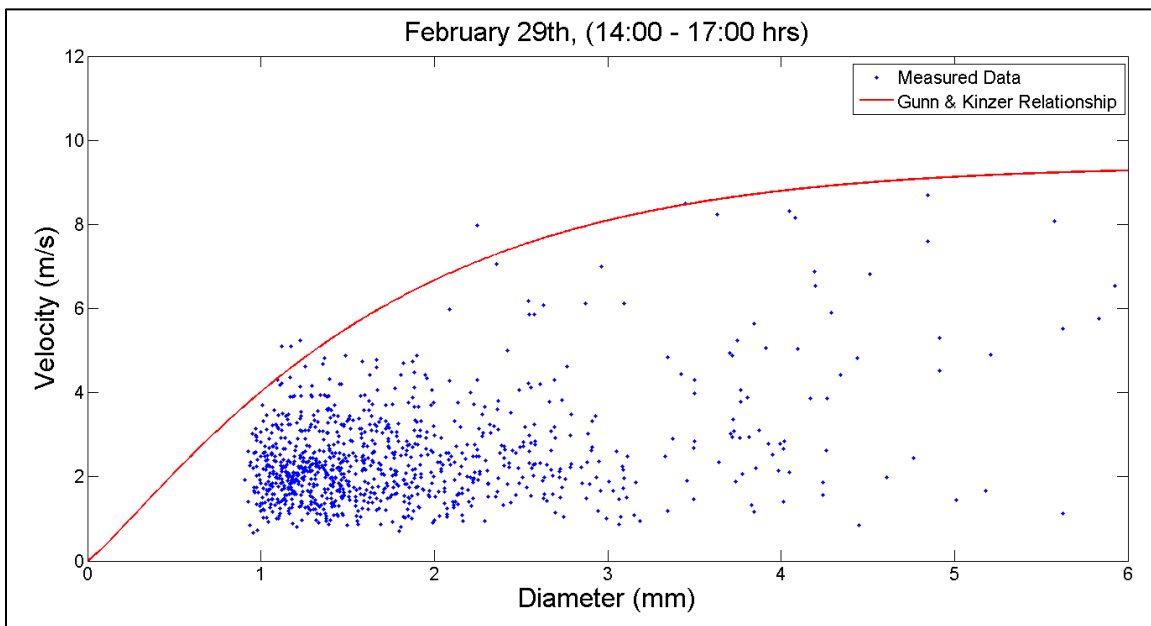


Figure 33 - The velocities of snowflakes compared against the Gunn & Kinzer Relationship.

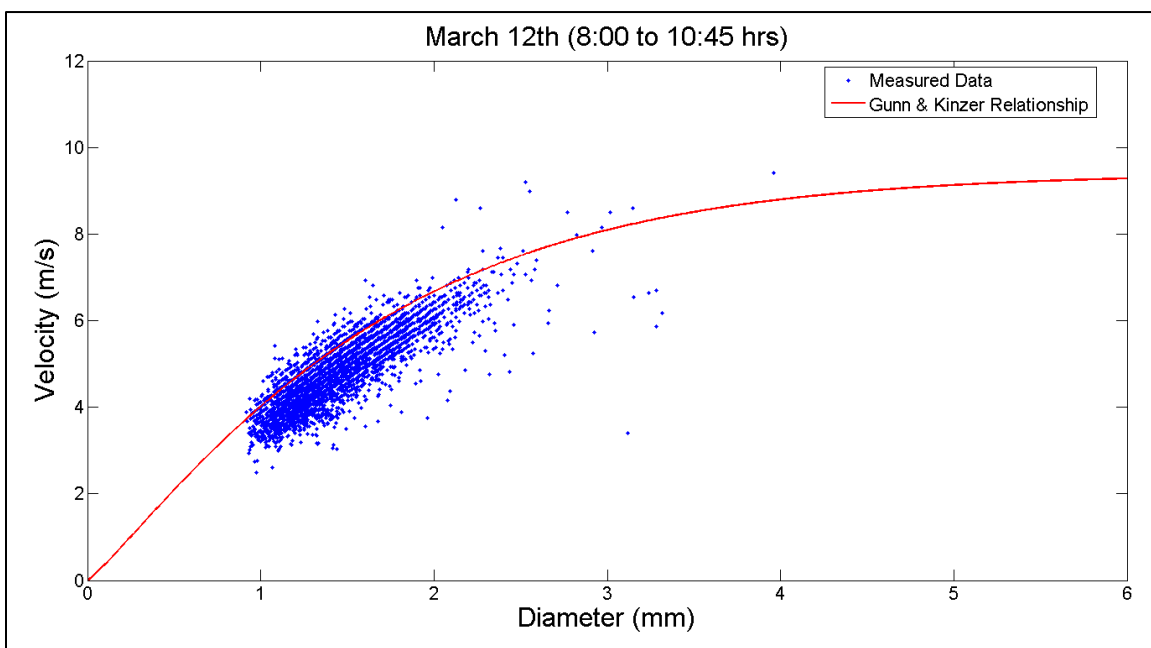


Figure 34 - The velocities measured during the March 12th rain event compared against the Gunn & Kinzer Relationship.

Discussion

Figure 29 and Figure 30 show that the new prototype detects rain at the same time as the tipping bucket, but the prototype does not signal snow at the same time as the tipping bucket. The tipping bucket was not designed to measure precipitation in the form of snow. The tipping bucket does signal precipitation during hour 20:00 on February 29th. The signal is due to the snow being trapped in the tipping bucket and melting which caused the tipping bucket to tip once.

The prototype consistently underestimates the magnitude of the rain rates compared to the rain rates captured by the tipping bucket. The two largest sources of errors leading to the underestimation is multiple drops in the sample area while another drop is being measured, and the limitation of not being able to estimate hydrometeors less than or equal to 0.9 millimeters. Another factor that may lead to consistent underestimation of rain rates is over estimation of the sample area. The sample area used is based upon the size the area between the detector head and lasers head. Because the laser diverges slightly, light in some areas is headed out of the sample area and is never detected by the detector. Similarly, light near the edges is not focused on the detector. Thus the sample is somewhat smaller than our estimate.

In order to capture small drops with slower velocities the prototype's settings were set to record 1500 measurements at a frequency of 66.6 kHz. Therefore, every time the prototype sensed a hydrometeor, there is a 0.0225 second window of time that another drop can enter the sampling area. An example of two drops being measured during one window of time can be seen in Figure 35. If more than one drop is recorded during this window of time, both of the drops were eliminated as errors. Errors of this type are referred to as simultaneous drops. Therefore, for every error due to simultaneous drops, two or more drops are not being included in the drop size distribution. The probability of this happening increases with increased rain intensity, which explains the larger differences between the rain rates measured by the prototype and tipping bucket during higher rain rates.

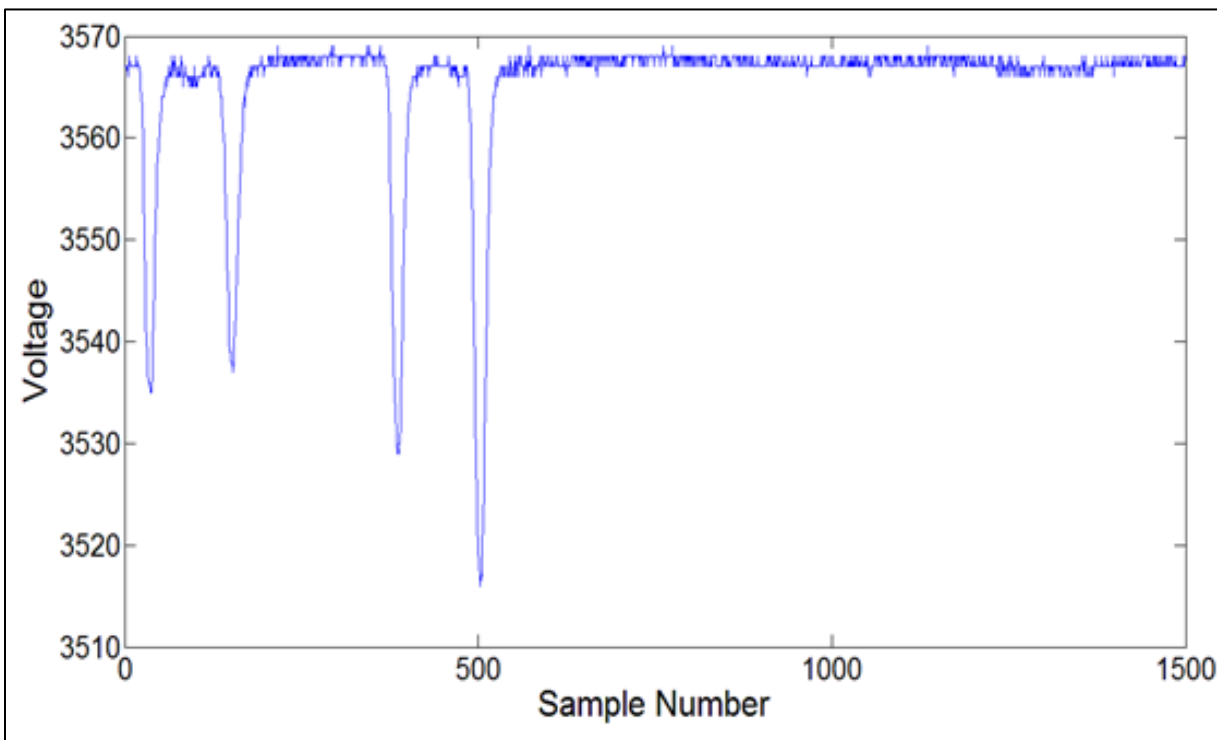


Figure 35 - An example of another drop entering the sample area during the same window of time a measurement takes place.

The number of drops analyzed as errors during the February 29th and March 12th rain events are shown in Table 5. Table 6 shows the number errors associated with simultaneous drops in the sample area and errors due to drops equal to or smaller than 0.90 mm.

Table 5 - The number of triggers and errors associated with each rain event.

| Rain Event Day | Hours | Number of Triggers | Total Number of Errors | Total Number of Drops Analyzed | % of Triggers as Errors |
|-------------------|--------------|-----------------------|---------------------------|-----------------------------------|----------------------------|
| February 29th | 0-2 | 10252 | 3269 | 6983 | 32 |
| March 12th | 8:00 - 10:45 | 5094 | 1378 | 3716 | 27 |

Table 6 - A table breaking down the number of simultaneous drops in the sample area and the number of drops smaller than 0.90 mm not included in the DSD.

| Day | Rain Event | Errors Due to Simultaneous Drops | Errors Due to Drops Smaller than 0.90 mm |
|---------------------------|--------------|----------------------------------|------------------------------------------|
| | Hours | | |
| February 29 th | 0:00 - 2:00 | 2484 | 785 |
| March 12 th | 8:00 - 10:45 | 778 | 600 |

Assuming that the number of simultaneous drops entering the sample area counts for two drops, the number of drops not included in the drop size distribution during the February 29th rain event is 5753. Therefore, the corrected number of drops that fell through the sample area is 12736. This means 45 percent of the drops recorded were eliminated as errors during the February 29th rain storm. This is a conservative estimate since it is assumed that only two drops were in the sample area when simultaneous drops were recorded. Using the same logic it was estimated that 37 percent of the drops during the March 12th rainstorm were not analyzed. This is consistent with the observation that the new prototype underestimates rain rates by just over a factor of 2.

The percentage of the total errors from drops with diameters less than 0.90 mm was 32 percent and 77 percent for the February 29th and March 12th rain events respectively. A possible reason for this difference is due to the type of rain event that occurred. The March 12th rain event was a light stratiform rain while the rain event on February 29th was a thunderstorm. Light stratiform precipitation is characterized by smaller drops while thunderstorms or convective storms have larger rain drops.

Another source of uncertainty is the assumption that the shapes of all rain drops are perfect spheres. Raindrops smaller than 1 millimeter are usually perfect spheres since intermolecular forces are strong enough to hold the drop in the shape of a sphere. As the size of raindrops increases, the drag force acting on the raindrops increases because of the larger frontal area. Thus the shapes of raindrops are deformed. The bottom edge of the raindrop becomes flat

while the lateral length of the raindrop elongates. The top of the drop remains rounded. The shape resembles a mushroom with no stem. The new prototype measures the longitudinal (vertical) length of raindrops which becomes shorter when rain drops are deformed. Using the longitudinal length and assuming the rain drop is a sphere leads to the underestimation of the true rain drop volume. A study by (Jones, 1959) showed that the average ratio between the longitudinal length and lateral length of a 2 mm drop was 0.99; a 3 mm drop was 0.92; and a 4 mm drop was 0.85. Assuming a 3 mm drop diameter is underestimated by 4 percent, half the difference of the ratio (longitudinal to lateral length) from one for a 3mm drop found by Jones would lead to a 12 percent underestimation of the volume for a drop.

The velocities of the hydrometeors measured by the new prototype fell closely to the theoretical Gunn and Kinzer relationship for the February 29th and March 12th rain events. The Gunn and Kinzer Relationship was determined in a laboratory in stagnant air whereas the velocity measurements recorded by the prototype were taken outdoors in a dynamic environment where updrafts, and downdrafts occur. An updraft would decrease the measured velocity while a downdraft would increase the velocity. Therefore, the scatter in the velocity measurements was expected. The velocities measured during the snow event were much lower than the Gunn and Kinzer Relationship. This was expected since snow flakes are less aerodynamic and less dense than water droplets .

Outdoor Testing Conclusions

The prototype was placed outdoors on the roof of the Wind Tunnel Annex from February 20th to March 13th. Two rain events and one snow event were captured by the prototype. The new prototype underestimated the rain rates compared to the rain rates measured by the tipping bucket by a factor of just over two. Furthermore the prototype's underestimation of the measured rain rates increased with increased rain rates. Rain drops smaller than 0.90 mm and drops occupying the sample area simultaneously were the two main errors contributing to the underestimation of the rain rates. It was estimated that 45 percent of the drops were not analyzed

during the February 29th rain event, and 37 percent of the drops were not analyzed during the March 12th rain event.

The velocities measured by the new prototype compared well with the relationship developed by Gunn and Kinzer. The scatter in the measured data was expected due to the dynamic environment in which the measurements were taken.

CHAPTER 7

CONCLUSION

A new instrument that measures the diameter and velocity of hydrometeors was redesigned, constructed, and tested. The redesigned instrument was based off of previous prototypes built by Michael Cloos. The new prototype has the advantage of being able to be repaired or adjusted if an internal component fails or becomes misaligned. Additionally a new data analysis method was developed during this project. The instrument and data analysis method were tested after the instrument was constructed.

Two controlled lab experiments were performed to assess the accuracy and precision of velocity and diameter estimates made by the new prototype. The first experiment consisted of dropping one hundred and fifty steel spheres with diameters of 0.98 mm, 1.98 mm, 2.98 mm, 3.98 mm, 4.98 mm, and 5.98 mm through the sample area of the new prototype. The 0.98 mm diameter spheres had a 12.4 percent average fractional error, the largest of the diameters tested. The 5.98 mm diameter spheres had the lowest average fractional error, 1.89 percent. The average fractional error decreased with increasing diameter size.

The average error of the velocity measurements compared to the calculated theoretical velocity ranged from -3.3 to -0.27 percent. The primary reason the measured velocities are slightly lower than the theoretical velocities was because the drag force was assumed zero in the theoretical calculations. The 0.98 mm trials had the largest average error of -3.3 percent. The 0.98 mm spheres were dropped by hand from a lower height since the mechanical device did not work for the 0.98 mm spheres. The fractional percent errors of the velocity measurements for each diameter tested ranged from 0.58 to 0.84 percent which was in good agreement with the estimated fractional error of 0.5 percent.

The second lab experiment performed was the Drip Experiment. The Drip Experiment consisted of dropping 25 milliliters of water through the sample area in the form of water droplets. The estimated volumes from all 22 trials underestimated the actual volume of water by

an average of $2.7 \text{ mL} \pm 1.18 \text{ mL}$. The average error was 10.79 percent which was reasonable considering that any errors in estimating the diameters are magnified to the power of three and summed over an average of 476 drops per trial.

Lastly, the instrument was placed outside to test the durability of the instrument, and to assess the accuracy of the instrument during precipitation events. The instrument was placed on the roof the University of Iowa Wind Tunnel Annex from February 20th, 2012 to March 14th, 2012 approximately 30 feet from an Iowa Flood Center Tipping Bucket. The new prototype never failed mechanically because of the elements while being outdoors. Two rain events and one snow event were captured during the outdoor campaign. The new prototype signaled precipitation at the same times as the tipping bucket but underestimated the magnitude of the rain rates compared to the tipping bucket by a factor just over 2. The primary reasons for the underestimation were due to errors from multiple drops occupying the sample area simultaneously and the data analysis limitation of not being able to estimate diameters smaller than or equal to 0.90 mm. The new prototype did signal precipitation during the snow event while the tipping bucket did not. The tipping bucket was not designed to measure snow. The diameters of the hydrometeors measured during the snow event had no meaning since the relationship between the size of a snowflake and the pulsed signals has not been investigated.

The velocities from the two rain events and the snow events were compared against Gunn and Kinzer Relationship which relates the terminal velocity of droplets to their diameter. The two rain events agreed well with the theoretical relationship while the majority of the velocities estimated during the snow event were smaller than the theoretical Gunn and Kinzer curve. This was expected since snowflakes are less aerodynamic and less dense than water droplets. The scatter of the data most likely occurred from the measurements being measured in a dynamic environment where downdrafts and updrafts happen. The upward or downward movement of air affects the velocities of hydrometeors.

The lab experiments and outdoor testing periods are evidence that the new prototype is capable of measuring the velocities and diameters of hydrometeors. However, over the duration

of this project, additional issues with the data collection, data analysis, and instrument were identified. To further improve the instrument the following issues should be addressed.

Issues to Be Addressed

The first issue that should be addressed is increasing the signal to noise ratio. This could be done by performing a DC offset on the signal to remove the background noise and then amplifying the signal. This would enhance the processing of the raw data by removing the ambiguity when determining the time of attenuation or the half-max time of attenuation. In particular, increasing the signal to noise ratio would enhance the ability to process drops equal to or smaller than 0.90 mm. The small pulsed signals should not be stair stepped shaped and could be analyzed by fitting Equation 4.18 to the end of the pulsed signals as described in Chapter 4. Furthermore, by increasing the signal to noise ratio, the accuracy of determining the time of attenuation, t_{att} , from the raw data could possibly be increased. Then the theoretical diameter calculation method described in Chapter 4 could be used to estimate the diameters. The advantage of the theoretical diameter calculation method is that a data reduction curve would not have to be developed.

The next issue that needs to be resolved is the errors associated with two or more rain drops occupying the sample area simultaneously. Currently, when the instrument detects a hydrometeor in the sample area, the data collection algorithm takes 1500 measurements at a frequency of 66.6 kHz. This creates dead time of 0.0225 seconds after each hydrometeor enters the sampling area. Previous work by Cloos indicated that taking 500 measurements was too short because, for very small drops, the second pulsed signal corresponding to a hydrometeor passing through the second laser sheet was not recorded by the instrument. This error was more prevalent for small hydrometeors because small hydrometeors tend to have slower velocities, which in turn take more time to pass by both laser sheets. In order to decrease the number of these errors, an improved data collection algorithm needs to be developed. One idea is to have the data collection algorithm quit taking samples after the second pulsed signal is fully captured. This would reduce

the dead time which would reduce the probability of multiple drops being measured during the same window of time. Another idea is to include a dead time analysis as Knoll describes in his book Radiation Detection & Measurement in order to account for the hydrometeors not being measured during the dead time.

Lastly, a detailed map of the actual sample area of laser light the photo detector sees should be developed. As of now the sample area was taken as the area between the detector head and laser head. It is hypothesized that the sample area could be smaller than the sample area used during this project. The divergence of some of the laser light near the edges is headed out of the sample area and is never detected by the photo detector. Similarly, light near the edge of the sample area is not focused on the detector. Understanding the actual sample area seen by the photo detector will remove one more of the uncertainties.

In conclusion, a new instrument that measures precipitation was designed, constructed, and tested. The instrument was capable of measuring the diameter and velocity of individual raindrops during precipitation events. The prototype has the potential to become a useful meteorological instrument by resolving the issues discovered over the duration of this project.

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